# COMPARISON OF RADIOMETRIC AND CHEMOMETRIC SENSITIVITIES FOR HETERODYNE AND DIRECT DETECTION DIAL

Daniel C. Senft, et al.

**July 2004** 

**Final Report** 

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#### 14. ABSTRACT

The heterodyne / direct detection DIAL comparison (HD/DD DC) experiment series was conducted at Kirtland AFB, NM, to simultaneously characterize and compare the radiometric and chemical detection sensitivities of heterodyne and direct detection DIAL systems. The system developed by the Air Force Research Laboratory Directed Energy Directorate demonstrated the first known programmable and shot-to-shot wavelength-agile heterodyne DIAL measurements. The experiments studied radiometric issues, speckle mitigation through spread spectrum (modelocked) operation, and chemical detection sensitivities. The measurements were performed over horizontal paths at standoff ranges from 4 to 15 km, using both natural and man-made targets. Heterodyne and direct detection radiometric and chemometric results are presented and contrasted, and are compared with predictions from simulations and models.

#### 15. SUBJECT TERMS

Differential absorption lidar (DIAL), heterodyne lidar, wavelength agile DIAL, direct detection lidar, laser remote sensing, laser chemical detection

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#### **Abstract**

The heterodyne / direct detection DIAL comparison (HD/DD DC) experiment series was conducted at Kirtland AFB, NM, to simultaneously characterize and compare the radiometric and chemical detection sensitivities of heterodyne and direct detection DIAL systems. The system developed by the Air Force Research Laboratory Directed Energy Directorate demonstrated the first known programmable and shot-to-shot wavelength-agile heterodyne DIAL measurements. The experiments studied radiometric issues, speckle mitigation through spread spectrum (modelocked) operation, and chemical detection sensitivities. The measurements were performed over horizontal paths at standoff ranges from 4 to 15 km, using both natural and man-made targets. Heterodyne and direct detection radiometric and chemometric results are presented and contrasted, and are compared with predictions from simulations and models.

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#### 1. Introduction

#### A. Overview

The Heterodyne / Direct Detection DIAL Comparison (HD/DD DC) experiments were designed to provide a direct, simultaneous comparison of the radiometric and chemical detection sensitivities of the two receiver techniques. From October 1998 to September 2003, the HD/DD DC measurements were a main component of the Laser Remote Optical Sensing (LROS) program at the Air Force Research Laboratory Directed Energy directorate (AFRL/DE). In general, it is expected that heterodyne detection will have a significant radiometric sensitivity advantage (by a factor of approximately 10<sup>2</sup> to 10<sup>3</sup>) over direct detection. A key issue for heterodyne detection, however, is the sensitivity of the process to speckle, which affects the chemical detection sensitivity. For a direct detection system, it is possible to spatially average multiple speckles across the receiver aperture, thereby reducing the speckleinduced fluctuation in the received signal. For a common single-mode heterodyne receiver, the requirement of having a coherent phase front over the receiver aperture results in a speckle-limited single shot SNR of unity. For the HD/DD DC experiments, a speckle mitigation technique was studied which uses a spread spectrum (modelocked) transmit waveform. In this technique, multiple laser longitudinal modes are transmitted, each of which is speckled independently when returned from a diffuse target with sufficient longitudinal extent. An illustration of the SNR characteristics versus range for each of these techniques is given in Figure 1. The values in the Figure were not calculated for specific systems, but are representative of heterodyne and direct detection systems with similar transmit energies and receiver apertures. A common characteristic of all of the techniques is that at short ranges the SNR will be speckle limited, and therefore mainly independent of range. At some distance, the SNR will become signal limited, and will decrease proportionally with the range squared (R<sup>2</sup>), or faster. The heterodyne radiometric advantage is that the breakpoint between specklelimited and signal-limited operation will occur at significantly greater ranges. The SNR advantage at short ranges in the speckle-limited regime seen for a direct detection system in comparison to a single-mode heterodyne system can be reduced or nearly eliminated by utilizing a spread spectrum transmit waveform. The cost of this improvement in comparison with the more common single-mode heterodyne systems is slightly more complexity in the front end of the heterodyne receiver, where a higher bandwidth capacity is required. This bandwidth can later be reduced by either analog or digital processing to a level similar to that of a single-mode heterodyne receiver. The complexity of the spread spectrum (modelocked) transmitter actually tends to be less than that of a wavelength-agile single-mode transmitter. At short ranges a direct detection system will always have an advantage over a heterodyne system, since direct detection can utilize both spatial averaging and spread spectrum operation to provide speckle mitigation, while heterodyne detection can utilize spread spectrum operation but not spatial averaging. The heterodyne system advantage will always occur for longer range operation, where heterodyning can continue to make measurements after the direct detection system return level has dropped below the system noise floor.

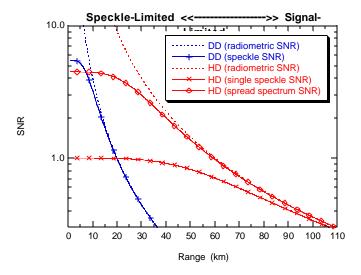


Figure 1. Illustration of spread spectrum heterodyne, single-mode heterodyne, and direct detection SNRs as a function of range.

### B. Development Timeline

The Heterodyne / Direct Detection DIAL Comparison (HD/DD DC) experiments utilized components from two separate systems, the Laser Airborne Remote Sensing (LARS) and Coherent Remote Optical Sensing System (CROSS). The LARS program demonstrated the capability of direct detection DIAL measurements from an airborne platform, achieving multiple chemical detection at a one-way standoff slant range of greater than 30 km (see Figure 2)². As the LARS program was concluding, the CROSS efforts began to develop a heterodyne DIAL capability, with the eventual goal of extending the operational range to a one-way standoff slant range of greater than 80 km. The development timeline for the LARS and CROSS systems is shown in Figure 3. The primary development required for the CROSS program was a wavelength agile, stable CO² local oscillator capable of high pulse repetition frequency (PRF) operation (with an eventual PRF goal of greater than 1 kHz). The Wavelength Agile Local Oscillator (WALO) was developed to meet the goals of the CROSS system³, and is discussed in more detail later in this report.

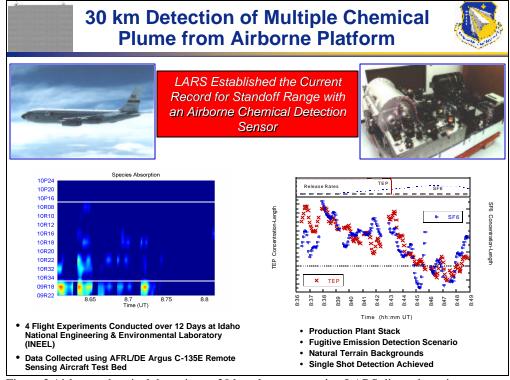


Figure 2.Airborne chemical detection at 30 km slant range using LARS direct detection system.

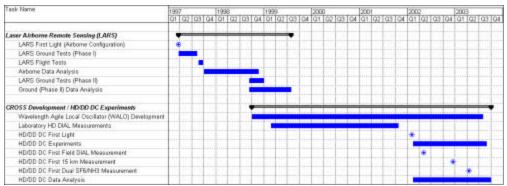


Figure 3. Development schedule for LARS, CROSS, and HD/DD DC experiments.

### 2. Experimental Information and Configuration

## A. HD/DD DC Equipment Description

The layout of the equipment used in the HD/DD DC experiments is shown in Figure 4. The various subcomponents will be described in more detail in the following sections. A common transmitter was used as the illumination source for both the heterodyne and direct detection receivers. The transmitted light was passed through a gas absorption cell, and the optical return signal for both receivers also passed through the gas cell.

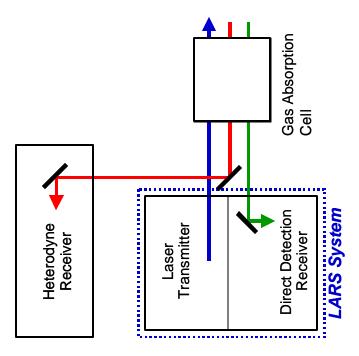


Figure 4. Layout of transmitter, direct detection receiver, and heterodyne receiver for Heterodyne / Direct Detection DIAL Comparison (HD/DD DC) experiments.

### B. Transmitter System

The Breadboard Oscillator (BBO)  $\mathrm{CO}_2$  laser developed by Textron Systems Corporation was utilized as the transmitter for the Heterodyne / Direction Detection DIAL Comparison (HD/DD DC) experiments. The BBO laser was also used in the Laser Airborne Remote Sensing (LARS) program, which developed an airborne direct detection DIAL system that demonstrated simultaneous detection of multiple chemicals at ranges of greater than 30 km (see Figure 2). The laser and associated cavity optics are shown mounted on the left-hand side of the LARS airborne optical bench in Figure 5. The BBO laser is an RF-excited transverse electric

atmospheric (TEA) CO<sub>2</sub> laser with output pulse energies of greater than 4 J on strong CO<sub>2</sub> transition lines, and a pulse repetition frequency (PRF) of up to 30 Hz. For the HD/DD DC experiments the laser PRF was limited to approximately 1 Hz by the capabilities of the data acquisition and control system. The laser uses a mechanical grating to change the output wavelength in a programmed sequence. The HD/DD DC experiments commonly utilized sequences consisting of 12 to 13 of the approximately 60 laser lines accessible by the BBO using the <sup>12</sup>Cl<sup>6</sup>O<sub>2</sub> isotope in the laser gain medium. To investigate speckle mitigation the laser operation was often alternated between non-modelocked and modelocked configurations for successive data sets. In both configurations the laser had multiple longitudinal mode output, but modelocked operation resulted in more longitudinal modes, with higher and more stable amplitudes. The key parameters for the BBO laser are given in Table 1.

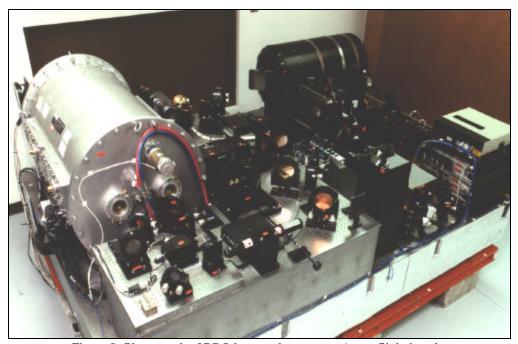


Figure 5. Photograph of BBO laser and system on Argus flight bench.

### C. Direct Detection Receiver

A diagram of the LARS bench, comprising both the laser transmitter and the direct detection receiver, is shown in Figure 6. The transmit optical path is shown in blue, and is primarily on the left side of the optical bench. The direct detection receive signal is shown in purple on the right side of the optical bench. The direct detection receiver utilizes a 16" diameter reflective telescope, with a secondary / pickoff mirror obscuration. The receive light is focused onto a 0.500 mm diameter liquid nitrogen cooled HgCdTe detector with a bandwidth of 80 MHz. The

signal from the detector is sampled at 60 MSa/s, and stored by the LARS Acquisition and Processing System (LAPS) for use in both quick-look and offline analysis.

**Table 1. BBO Laser Key Parameters** 

Parameter	Value	
CO <sub>2</sub> Isotope	$^{12}C^{16}O_2$	
-	$^{13}C^{16}O_2$	
Pulse Energy	$>$ 4 J (strong line, using $^{12}C^{16}O_2$ )	
	> 50 mJ (weak line)	
Pulse Repetition Frequency	30 Hz (maximum)	
	10 Hz (nominal)	
	1 Hz (HD-DD DC experiments)	
Wavelength Tuning Capability	Single shot	
Number of Accessible Wavelengths	$\sim 60  (^{12}\text{C}^{16}\text{O}_2  \text{isotope})$	
	$\sim 50  (^{13}\text{C}^{16}\text{O}_2  \text{isotope})$	
Pulse Type	Gain switch spike with relaxation tail	
Pulse Width	~ 10 μs (non-modelocked)	
	~ 6 μs (modelocked)	
Beam Divergence	~ 1.0 mrad (from laser)	
_	0.285 mrad (transmitted downrange)	

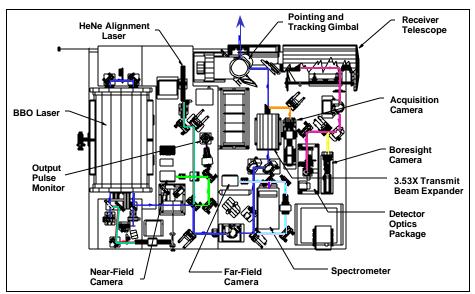


Figure 6. Plan view of laser transmitter and direct detection receiver.

### D. Wavelength Agile Local Oscillator (WALO)

The Wavelength Agile Local Oscillator (WALO) was developed for stable wavelength agile operation at high PRFs (> 20 Hz). The WALO uses a cavity waveguide for the CO<sub>2</sub> gain medium, with acousto-optic modulators (AOMs) inside the laser cavity for wavelength tuning. Prior wavelength agile CO<sub>2</sub> local oscillators had used mechanical tuning of diffraction gratings, which tended to be unstable at high PRF operation (> 20 Hz), due to the mechanical settling time of the moving grating fixture. The WALO utilized paired AOMs to achieve high PRF, stable wavelength agile operation. Since the AOMs utilize acoustic waves to change the wavelength of light transmitted, the tuning time limit was determined by the propagation time of the acoustic wave in the transverse direction across the AOM, and the stabilization time of the CO<sub>2</sub> laser into CW operation. Tuning rates of 500 Hz were demonstrated with the WALO, which was well beyond the tuning capability of the transmitter laser used in the HD/DD DC experiments. Tuning rates of many kHz have been demonstrated by other research groups utilizing AOMs with CO<sub>2</sub> waveguide lasers, so the tuning rates used for the WALO are not at the limits for this type of technology. Since there are no moving parts in the design, the WALO is relatively robust, and well suited to operation in both field and airborne environments.

## E. Heterodyne Receiver

The CROSS heterodyne receiver is shown in Figure 7. The receive signal and WALO beams are combined using a beam splitter, and are focused onto a 0.100 mm x 0.100 mm square HgCdTe detector with a bandwidth of 800 MHz.

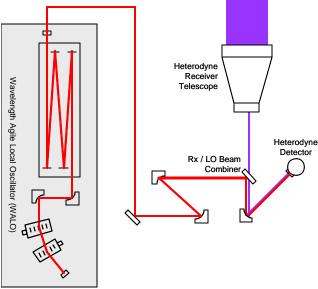


Figure 7. Layout of heterodyne receiver with Wavelength Agile Local Oscillator (WALO).

#### F. Gas Cell

The gas cell used in the HD/DD DC experiments (see Figure 8) is a 4' x 4' x 4' aluminum cube, with IR-transmissive polyethylene windows on two sides. The gas cell was designed for both gas and liquid chemical insertion. Gas valves are incorporated into the side panels, and a funnel mechanism with heated Petry dish is mounted on the top panel to evaporate chemicals inserted in liquid form. Fans are mounted inside the cell to provide uniform mixing of the chemicals inserted. The cell has been used with gaseous sulfur hexafluoride (SF<sub>6</sub>), gaseous ammonia (NH<sub>3</sub>), and liquid ammonium hydroxide (NH<sub>4</sub>OH). For the HD/DD DC experiments, only the chemicals in gaseous form (SF<sub>6</sub> and NH<sub>3</sub>) were used. Insertion of gaseous chemicals was performed by filling sample cylinders with pure gas to above the ambient atmospheric pressure. The sample cylinders were connected to valves on the side of the gas cell (note sample cylinder attached to valve on right side of cell in Figure 8 photo), which were opened at the desired point in the experiment to insert the excess pressure from the sample cylinders into the cell. After a few seconds the valves were again closed, to prevent all of the gas in the sample cylinders from leaking into the cell. Although this insertion procedure is not extremely precise, it provides a relatively simple method to achieve reasonably predictable and repeatable results. From viewing the DIAL absorption plots, it appears that the internal cell fans cause complete mixing of the chemicals in the cell within 10 sec. The quick-release door panels were removed to rapidly evacuate the inserted chemicals between data sets.

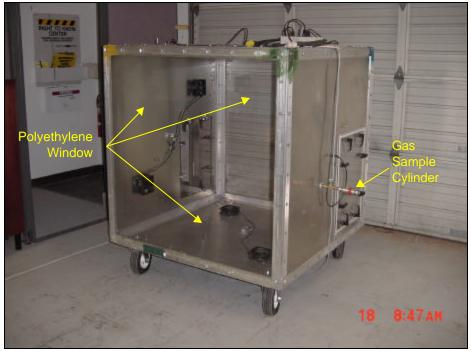


Figure 8. Photograph of 4' x 4' x 4' gas cell.

# G. Target Sites

Target sites at one-way ranges of 4.320 km (4KS), 7.460 km (7KS), and 14.9 / 15.3 km (15KS) were developed for use in the HD/DD DC experiments. Other target sites were also available at approximately 2 km (2KS), 5 km (5KS), and 6 km (6KS), but were not used in the HD/DD DC experiments, other than for alignment purposes. Figure 9 shows the beam paths from the transmitter location in Building 770 (B770) on Kirtland AFB, to the various target sites. The

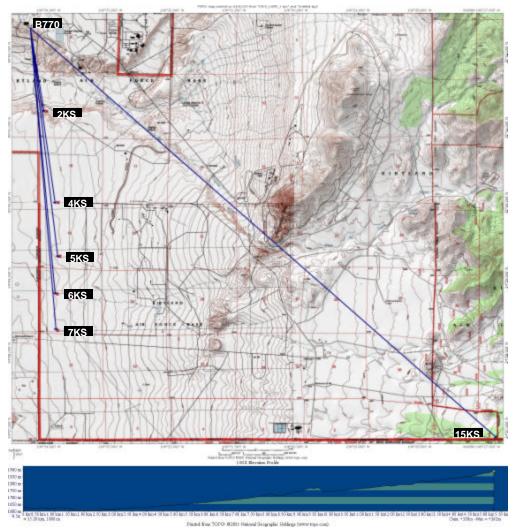


Figure 9. Topographic map with beam paths (blue arrowed lines) from B770 to 2KS, 4KS, 5KS, 6KS, 7KS, and 15KS sites. The elevation profile from B770 to the 15KS target is shown below the map.

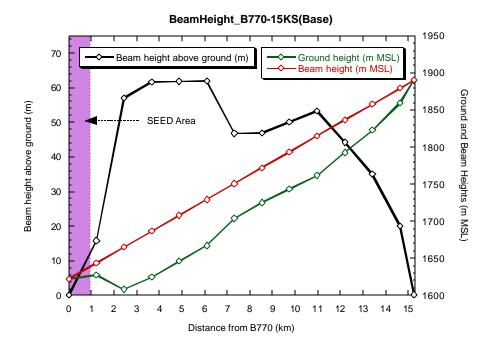


Figure 10. Beam height and elevation profile from B770 to the 15KS target.

propagation paths to all of the target sites were within 5° of horizontal, and within 100 m of the ground at all locations along the paths. The elevation profile from B770 to the 15KS target is also shown at the bottom of Figure 9, and is representative of the general elevation profile characteristics for all of the target sites. A more detailed plot showing the beam height and elevation profile from B770 to the 15KS target is given in Figure 10. A weather station was operated next to B770 to provide atmospheric pressure, temperature, and humidity measurements during the experiments. This information was input into HITRAN-PC, which was then used to calculate the expected atmospheric transmission along the propagation path.

Photographs of the target sites are shown in Figures 11-15. Figure 11 shows blueboard and flame-sprayed aluminum (FSA) targets at the 2KS site used for pointing alignment and system calibration. Figure 12 shows the blueboard and berm area targets at the 4KS site. At the time the photograph in Figure 12 was taken, only a single blueboard target was present. In early April 2003 another blueboard target using non-weathered blueboard panels was constructed and placed between the old blueboard target and berm illumination locations. Aluminum alignment targets and the berm illumination area for the 7KS site are shown in Figure 13. The 15KS blueboard target is shown in Figure 14. Two different 15KS target sites were used during the HD/DD DC experiments. The first 15KS site was located at ~ 14.9 km, and was used

until the end of 2002. The second 15KS site was located at  $\sim 15.3$  km, and was used starting in 2003. The great majority of the experimental measurements were conducted using the second site, and all 15KS information given in this report pertains to this location, unless specifically stated otherwise. A photograph of the propagation path from B770 to the 15KS target board is shown in Figure 15.



Figure 11. Photographs of left and right sides of the 2KS site, showing the blueboard target (left, 8' x 8') and flame-sprayed aluminum (right, 4' x 4') calibration targets.



Figure 12. Photograph of 4KS target site, showing blueboard target (right of photograph) and approximate berm illumination area (yellow circle, not exactly to scale). In April 2003 a second target using non-weathered

blueboard panels was constructed and placed on the berm (yellow rectangle).



Figure 13. Photograph of 7KS target site, showing aluminum (right) and plywood (left) calibration/pointing target boards and approximate berm illumination area (yellow circle, not exactly to scale).

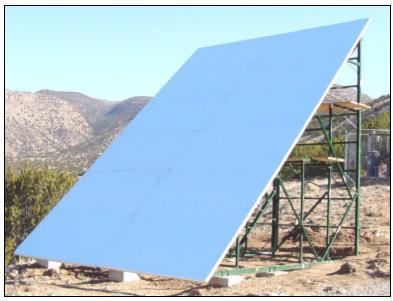


Figure 14. Photograph of 15KS blueboard target.



Figure 15. Photograph of propagation path from B770 to 15KS blueboard target.

Panels of blueboard insulation (8' x 4' x 2") were specially prepared for use at the target sites. The preparation method consisted of removing the external extruded surface using a 120-grit belt sander, thereby exposing the diffuse high reflectivity internal material. It was necessary to remove the external surface on all surfaces to prevent warping of the blueboard sheets. The dimensions of the blueboard target at the 4KS site were 12' long by 8' wide', and the target was placed at approximately a 60° angle of incidence, resulting in a 6' long x 8' wide target cross section. The beam diameter at the 4KS target is approximately 4' (285  $\mu$  4 full-angle divergence in output space) to the second null of the transmitted beam far-field distribution, which includes ~ 85% of the total beam energy. The blueboard target at the 15KS site was 24' length x 16' width at a 45° angle of incidence, resulting in a 17' x 16' target cross section. The beam diameter at the 15KS target is approximately 9' to the second null of the far-field distribution.

Dirt berms were also used as targets at the 4KS and 7KS sites. The dirt berm reflectivity, calculated from calibrated direct detection measurements at the 4KS site, was determined to approximately match a Lambertian reflector with a total reflectivity of 3%, for angles from normal to near grazing incidence. For the approximate incidence angle of 60° for the berms, the reflectivity is therefore approximately 0.005 sr¹. The blueboard and berm solid-angle reflectivities are given in Table RR1 for the various target angles used in the HD/DD DC experiments. The blueboard provides a high reflectivity for 10 µm radiation, and the reflectivity does not decrease as quickly with increasing incidence angle as would occur for a Lambertian target. It should also be noted that the blueboard reflectivities were measured in the laboratory immediately after the blueboards were prepared. The radiometric results which will be presented later in this report suggest that the blueboard reflectivity decreased significantly as the boards weathered, since they were continuously exposed to the outside elements once they were installed at the target sites. Laboratory reflectivity measurements have not been conducted on the weathered blueboards.

Table 2. Blueboard and dirt berm reflectivities

Target	Incidenc	Reflectivity
Material	e	(sr <sup>-1</sup> )
	Angle	
Blueboard	0°	0.094
Blueboard	45°	0.070
Blueboard	60°	0.064
Dirt berm	60°	0.005

### 3. Transmit and Receive Temporal and Frequency Characteristics

A detailed understanding of the temporal and frequency characteristics of the laser transmit and receive signal is required to develop accurate analysis procedures. The modelocked (spread spectrum) operation implemented to provide speckle mitigation in the heterodyne DIAL measurements differs significantly from the more commonly used single-mode heterodyne technique, and necessitates more demanding system requirements (primarily the ability to record wideband heterodyne signals, rather than narrowband signals centered on the heterodyne intermediate frequency). The signal-to-noise ratio (SNR) advantages of narrowband operation can be recovered in post-processing of the wideband signals, because of the frequency-fence structure of the laser modes. As will be shown, the laser frequency modes are narrow, and occur at spacings determined by the laser cavity length, allowing the processing bandwidth to be reduced to only those regions where the return signal occurs. Since most of the measurements reported in this paper have reasonably good heterodyne SNR values, this processing bandwidth reduction was studied, but was not implemented for the analysis results presented.

#### A. Modelocked Characteristics

The temporal and temporal frequency characteristics for a single outgoing modelocked laser pulse are shown in Figure 16. The outgoing (monitor) pulse characteristics were captured using direct detection of a small portion (< 1%) of the outgoing beam energy. Figure 16(a) shows the common CO<sub>2</sub> laser temporal pulse shape, which is composed of a gain-switch spike and a relaxation tail. An expanded view showing the modelocked pulse train is given in The temporal frequency power spectrum showing the multiple cavity longitudinal modes for the direct detection monitor pulse is shown in Figure 16(c). The modelocked characteristics are achieved by placing into the BBO laser cavity an acoustooptic modulator (AOM) with a sinusoidal variation which matches the cavity round-trip time. The AOM sinusoidal variation forces the laser cavity longitudinal modes to be in phase with each other, resulting in the modelocked temporal pulse train. Modelocking also tends to generate more longitudinal cavity modes with more stable amplitudes than allowing the laser to free-run with multiple longitudinal modes (as will be seen in Figures 19 to 21). The variations from perfect theoretical modelocking operation seen in the BBO laser pulses are believed to result mainly from the gradual degradation of the optical coatings on the intracavity AOM. The AOM was coated primarily for operation at 11.15 µm (<sup>13</sup>C<sup>16</sup>O<sub>2</sub> 10P20), but was primarily used in the HD/DD DC experiments over the wavelength range 10.25 to 10.70 μm. In addition, the AOM is an element in an open-air laser cavity, and is therefore in a high energy density region which is not completely protected from dust particles and contaminants. An increase in the visible degradation of the optical coating and in the difficulty in obtaining optimal modelocking operation was noted during the progress of the experiments, starting with the insertion of the modelocker in January 2002, and continuing until the final experiments in August 2003.

The received temporal heterodyne signal for modelocked operation is shown in Figure 17(a), with an expanded version shown in Figure 17(b). Since the transmitted modelocked laser beam contains multiple longitudinal modes, the transmit laser and local oscillator were not frequency locked, and multiple intermediate frequencies (up to 100's of MHz) are present in the heterodyne signal. The heterodyne modulation of the modelocked micropulses is especially evident in Figure 17(b).

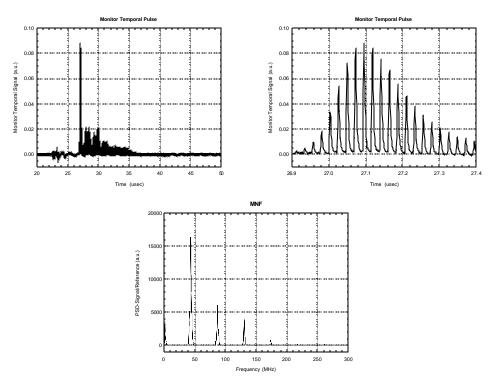


Figure 16. Modelocked laser temporal pulse (direct detection). (a) entire pulse waveform, (b) expanded time scale, (c) temporal frequency spectrum.

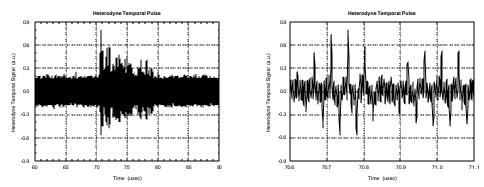


Figure 17. Heterodyne receive signal from a modelocked laser pulse. (a) entire pulse waveform, (b) expanded time scale.

Heterodyne temporal frequency spectra for modelocked operation are shown in Figure 18. The superimposed heterodyne spectra of the signal and local oscillator [calculated from 70-83 µs in Figure 17(a)] are shown in Figure 18(a). The homodyne spectra for the local oscillator [calculated from 61-66 µs in Figure 17(a)], with the DC component removed, are shown in Figure 18(b). The local oscillator output actually consists of a dominant single longitudinal cavity mode, with two smaller features, which are denoted as 'spurs'. The spurs occur at the single and double AOM frequency shifts (approximately 77 and 154 MHz). They are believed to result from slight impurities in the local oscillator dual intra-cavity AOMs, which causes some of the unshifted (in wavelength) beam to be scattered into the direction of the shifted beam. Since this can happen in both of the AOMs, the local oscillator output can consist of three frequencies, the desired frequency, a single-shifted frequency, and a double-shifted frequency. The exact frequency shifts are slightly different for each local oscillator wavelength, since the AOM frequency shift required is dependent upon the output wavelength desired.

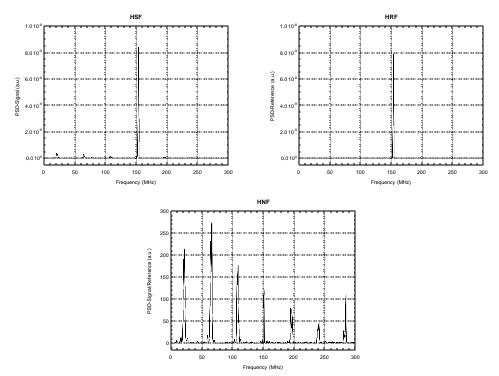


Figure 18. Heterodyne receive signal temporal spectra from a modelocked laser pulse.

(a) signal + local oscillator, (b) local oscillator only, (c) normalized signal [(signal + local oscillator) / (local oscillator)].

The optical power in the spurs is more than 3 orders of magnitude less than that in the main local oscillator output, and would not be evident in most heterodyne measurements. In many laboratory or short-range heterodyne measurements, the return signal level would be much higher than that in the spurs. Also, for many heterodyne systems a single longitudinal mode transmitter is used, and the intermediate frequency and associated receiver passband would be significantly lower than the first spur frequency. In the case of the HD/DD DC measurements, however, wideband heterodyne detection is required because of the multiple longitudinal mode (MLM) nature of the transmitter, and the received signal optical power levels are of the same order of magnitude as those of the local oscillator spurs. A number of physical methods to eliminate or significantly reduce the spurs were studied, but it was determined that a simpler and less costly option was to remove the spurs in the processing algorithms. The normalization procedure used for spur removal is described in more detail in the data processing section. It should also be noted that the noise level evident in Figure 17(a) is mainly caused by the 154 MHz beating of the main LO frequency component with the second spur, and not by the local oscillator shot noise.

The heterodyne signal temporal frequency power spectrum for modelocked operation is shown in Figure 18(c), after the normalization procedure has been applied. As seen in the Figure, the local oscillator spurs at approximately 77 and 154 MHz are removed by the normalization procedure, and only the transmit laser cavity modes are present. The laser cavity modes are separated by approximately 44 MHz, which corresponds to the cavity round-trip time (~23 ns for a 3.4 m laser cavity length). The double peak nature of the frequency modes in Figure 18(c) is believed to result from the DC wrap-around inherent in the periodogram computation process, with the negative frequency modes happening to nearly fall back onto the positive frequency modes. Multiple-peak modes can also result from the transmit laser containing some multiple TEM output, but this is not believed to be the case in this instance.

#### B. Non-Modelocked Characteristics

The temporal and temporal frequency characteristics for a non-modelocked output pulse are shown in Figure 19, similar to the presentation in Figure 16 for a modelocked pulse. The gainswitch spike and relaxation tail are again evident. A small after pulse (at 39-40  $\mu$ s in the plot), probably resulting from continued RF pumping during the pulse and incomplete cavity dumping, is also present for this specific pulse. The expanded scale in Figure 19(b) shows a significant difference between non-modelocked and modelocked operation. The effects of MLM operation are evident in the partial micropulse temporal structure, but the pulses are overlapped rather than distinct because the longitudinal cavity modes are not phase matched, as is the case in modelocked operation. The frequency modes are shown in Figure 19(c). Multiple modes are present, but as seen in comparison with Figure 16(c), there are fewer modes for non-modelocked operation, with a more rapid decrease in amplitude away from the main mode. This mode structure indicates that non-modelocked operation will result in some speckle mitigation, but not as much as for modelocked operation.

The heterodyne receive signal from the non-modelocked pulse is shown in Figure 20. The heterodyne modulation is evident in Figure 20(b), and follows the pulse envelope seen in Figure 19(b).

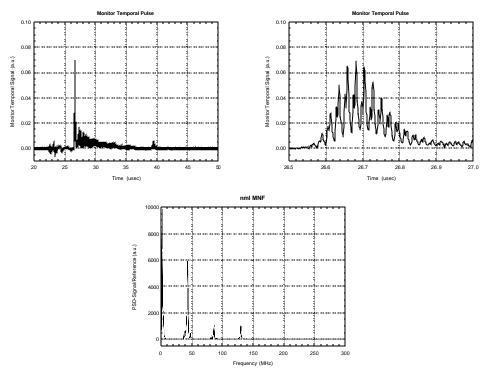


Figure 19. Non-modelocked laser temporal pulse (direct detection). (a) entire pulse waveform, (b) expanded time scale, (c) temporal frequency spectrum.

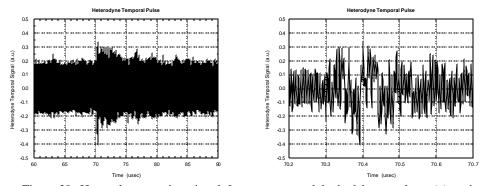


Figure 20. Heterodyne receive signal from a non-modelocked laser pulse. (a) entire pulse waveform, (b) expanded time scale.

The heterodyne signal spectra for non-modelocked operation are shown in Figure 21, in similar fashion to that for modelocked operation shown in Figure 18. In this case, the normalized spectrum shown in Figure 21(c) shows the effect of the DC wrap-around, where the set of frequency modes marked as (1) can be considered as the positive frequency modes, and those marked as (2) can be considered as the wrapped negative frequency modes. With this unwrapping, it can again be seen that the frequency mode spacing is approximately 44 MHz, as expected. Comparing Figure 21(c) and 18(c), it can be seen that the modelocked spectrum contains more modes with higher amplitudes than the non-modelocked spectrum, indicating that modelocked operation will result in a greater degree of speckle mitigation.

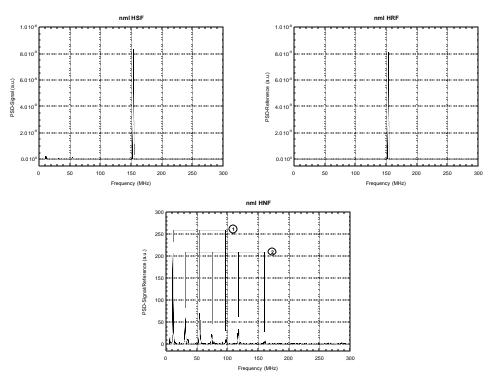


Figure 21. Heterodyne receive signal temporal spectra from a non-modelocked laser pulse. (a) signal + local oscillator, (b) local oscillator only, (c) normalized signal [(signal + local oscillator) / (local oscillator)].

### 4. Data Analysis and Results

#### A. Overview

As described previously, the development of the Coherent Remote Optical Sensing System (CROSS) began in October 1998, as the Laser Airborne Remote Sensing (LARS) program was nearing completion. Equipment development, laboratory system characterization and DIAL measurements, and preliminary open-air measurements were conducted during 1999, 2000, and 2001. Although the system continued to be upgraded and improved, the system components remained essentially the same after the HD/DD DC measurements began in February 2002. The data sets included in the radiometric, DIAL, and system characterization analyses for this report are shown in reverse chronological order in Appendix A, Table A1.

### B. Radiometric Theoretical Analysis

The differential absorption lidar (DIAL) technique utilizes the variations in absorption at different interrogation wavelengths to determine a 'spectral fingerprint' in order to detect and quantify chemicals in the laser path. In the simplest scenario, this can be thought of as a twowavelength system, with one wavelength tuned to an absorbing feature of a chemical, and the other wavelength used as a reference which is not absorbed. In a more general and realistic scenario, the DIAL problem can be posed in terms of using a sequence of N laser wavelengths to determine the concentrations for M chemicals. For the general case, the commonly presented 2-wavelength DIAL approach may not be usable, since the absorption of one chemical may interfere with either the on- or off-absorption wavelength of another chemical. It should be noted that conceptually there is no difference in the DIAL technique between measuring the concentrations (see Eq. 1) of the  $M_n$  atmospheric and  $M_n$  target gases, although more laser wavelengths are required to measure more gases. In the HD/DD DC experiments, the M<sub>a</sub> contributions were determined by measuring the atmospheric pressure, temperature, and humidity, and determining the expected atmospheric transmission ( $\tau_a$ ) using an atmospheric model (HITRAN-PC). The DIAL equation for using N laser wavelengths to measure M (specifically  $M_m$ ) target gases can be written in the following form

$$\begin{split} E_{r}(\lambda) &= E_{L}(\lambda) \eta_{x}(\lambda) \, \eta_{ov} \rho \left( \lambda \right) \Omega \eta_{r}(\lambda) \prod_{a=1}^{M_{a}} exp \Bigg( -2 \int_{0}^{R} \kappa_{a}(\lambda) \, C_{a}(R') \, dR' \Bigg) \\ &\times \prod_{m=1}^{M_{m}} exp \Bigg( -2 \int_{0}^{R} \kappa_{m}(\lambda) \, C_{m}(R') \, dR' \Bigg) \\ &= E_{L}(\lambda) \eta_{x}(\lambda) \, \eta_{ov} \rho \left( \lambda \right) \frac{A_{r}}{R^{2}} \tau_{a}^{2}(\lambda) \eta_{r}(\lambda) \prod_{m=1}^{M_{m}} exp \Big( -2 \kappa_{m}(\lambda) (CL)_{m} \Big) \end{split} \tag{1}$$

where  $E_r$  = return energy incident on detector

 $E_L$  = laser transmit energy

= system optical transmission efficiency  $\eta_{x}$ 

= overlap factor for transmitted beam footprint at the target, target size, and  $\eta_{ov}$ 

receiver field-of-view

ground reflectivity (per solid angle) solid angle subtended by the receiver Ω system optical receiver efficiency  $\eta_r$ 

total # of absorbing atmospheric gases  $M_a$ absorption coefficient of ath atmospheric constituent

concentration of a<sup>th</sup> atmospheric constituent  $C_a$ 

total # of absorbing target gases  $M_{m}$ 

absorption coefficient of m<sup>th</sup> target gas  $\kappa_{\mathrm{m}}$ 

= concentration of m<sup>th</sup> target gas  $C_{m}$ 

area of receiver  $A_r$ 

 $\kappa_a$ 

R = one-way range from transmitter to target

= one-way atmospheric transmission (includes absorption of all M<sub>a</sub>  $\tau_{\rm a}$ 

atmospheric constituents)

 $(CL)_{m} = \int_{0}^{R} C_{m}(R')dR'$ , concentration-length product for  $m^{th}$  target gas.

The above equation assumes a hard target is providing the return signal, and therefore a column-content measurement is being made. If a distributed target, such as the atmosphere or aerosols, provides the return mechanism, the received signal will be spread in time, and a range-resolved measurement will be made. The chemometric analysis is performed similarly for both column-content and range-resolved measurements, but must be done for each range window in the range-resolved case. Most long range systems utilize column-content measurements because of the significantly larger return signal level occurring from hard targets as compared to atmospheric or aerosol backscatter.

### C. Direct Versus Heterodyne Detection Signal Processing Issues

The differences in the physics of the detection processes between direct and heterodyne detection requires a complete and accurate understanding of the signal processing techniques that are used. One issue that needs to be considered in the heterodyne detection case, is that the commonly derived heterodyne SNR relation

$$SNR_{HD} = \eta_{qe} \frac{\langle P_r \rangle}{hv} \frac{1}{2B}$$
 (2)

for continuous wave heterodyne operation is not directly applicable to the case of a pulsed laser, where the signal will be integrated to provide a result proportional to the received energy  $E_r$ .

In the case of direct detection, the relationships between the current out of the detector  $I_{DD}$ , the instantaneous power received  $P_r$ , and the received energy  $E_r$  are given by

$$I_{DD}(t) \propto \left| \varepsilon_{r}(t) \right|^{2} \cong \left| a_{r}(t) \cos \left( \omega_{r} t + \phi_{r} \right) \right|^{2} \cong \frac{1}{2} \left| a_{r} \right|^{2} = P_{r}(t)$$

$$U_{DD} = \int_{\Delta T} I_{DD}(t) dt \propto \int_{\Delta T} P_{r}(t) dt = E_{r}$$
(3)

The measured value  $U_{DD}$  is the parameter required for both radiometric and DIAL analysis. Since it is proportional to  $E_r$ , it is then also directly proportional to the total transmission of the target gases of interest. The processing is actually more complicated than the simple relation given in Eq. 3, but the key relationship between  $U_{DD}$  and  $E_r$  is retained. The details of the processing are given in Appendix C, where the code for the primary direct detection Matlab calculation program DATREDUC.m is reproduced.

Determining an equivalent heterodyne parameter  $U_{HD}$  to the direct detection parameter  $U_{DD}$  is significantly more complicated. There are many different ways to calculate a  $U_{HD}$  parameter for heterodyne detection, all of which are valid (but not necessarily optimal) as long as  $U_{HD}$  is directly proportional to the received energy  $E_{\rm c}$ . In the case of heterodyne detection, the current out of the detector is given by

$$\begin{split} I_{HD}(t) &\approx \left| \boldsymbol{\epsilon}_{r}\left(t\right) + \boldsymbol{\epsilon}_{LO}\left(t\right) \right|^{2} = \left| \boldsymbol{a}_{r}\left(t\right) \cos\left(\boldsymbol{\omega}_{r}t + \boldsymbol{\phi}_{r}\right) + \boldsymbol{a}_{LO}\left(\cos\boldsymbol{\omega}_{LO}t + \boldsymbol{\phi}_{LO}\right) \right|^{2} \\ &\cong \left| \boldsymbol{a}_{r}\left(t\right) \right|^{2} \cos^{2}\left(\boldsymbol{\omega}_{r}t + \boldsymbol{\phi}_{r}\right) + 2\left| \boldsymbol{a}_{r}\left(t\right) \boldsymbol{a}_{LO} \right| \cos\left(\boldsymbol{\omega}_{r}t + \boldsymbol{\phi}_{r}\right) \cos\left(\boldsymbol{\omega}_{LO}t + \boldsymbol{\phi}_{LO}\right) \\ &+ \left| \boldsymbol{a}_{LO} \right|^{2} \cos^{2}\left(\boldsymbol{\omega}_{LO}t + \boldsymbol{\phi}_{LO}\right) \\ &\cong \frac{1}{2}\left| \boldsymbol{a}_{r}\left(t\right) \right|^{2} + \frac{1}{2}\left| \boldsymbol{a}_{LO} \right|^{2} + 2\left| \boldsymbol{a}_{r}\left(t\right) \boldsymbol{a}_{LO} \right| \cos\left[\left(\boldsymbol{\omega}_{r} - \boldsymbol{\omega}_{LO}\right)t + \left(\boldsymbol{\phi}_{r} - \boldsymbol{\phi}_{LO}\right)\right] \\ &\cong P_{r}\left(t\right) + P_{LO} + 2\sqrt{P_{r}\left(t\right)P_{LO}} \cos\left[\left(\boldsymbol{\omega}_{r} - \boldsymbol{\omega}_{LO}\right)t + \left(\boldsymbol{\phi}_{r} - \boldsymbol{\phi}_{LO}\right)\right] \\ &\cong 2\sqrt{P_{r}\left(t\right)P_{LO}} \cos\left[\left(\boldsymbol{\omega}_{r} - \boldsymbol{\omega}_{LO}\right)t + \left(\boldsymbol{\phi}_{r} - \boldsymbol{\phi}_{LO}\right)\right] \end{split} \tag{4}$$

The above derivation uses the facts that the heterodyne detector does not respond at optical frequencies, that the detector or electronics will not pass baseband (DC) signals (thereby removing the  $P_{LO}$  contribution), and that the local oscillator power  $P_{LO}$  is significantly larger than  $P_r$  (thereby removing the  $P_r$  term). The above relation has been significantly simplified, and a more complete relationship would need to include the contribution of the LO spurs, as seen previously in Figures 18(a) and 21(a). Since the optical power in the LO spurs is of the

same order of magnitude as the received instantaneous power  $P_r$ , the beat contribution between the spurs and the main LO mode is also present in the detector output, and occurs at harmonics of the AOM shift frequency (approximately 77 and 154 MHz). The presence of the LO spurs led to the construction of a customized processing technique designed to remove their effect in the calculation of  $U_{\rm HD}$ .

The calculation of  $U_{HD}$  is primarily based upon the use of the power spectral density of  $I_{HD}$ . The power spectral density  $S_{S+N}$  of  $I_{HD}$  is computed over a temporal window where the return and local oscillator signals are present, and a separate power spectral density  $S_N$  is computed over a temporal window where the local oscillator but no signal is present.  $U_{HD}$  is then calculated from the integration over temporal frequency space of the point-by-point normalization of  $S_{S+N}$  by  $S_N$ 

$$U_{HD} = \int_{\Delta F} \frac{S_{S+N}(f)}{S_{N}(f)} df - 1 - N_{ENF} = \int_{\Delta F} \frac{\left| \Im_{S+N} \left\{ I_{HD} \right\} \right|^{2}}{\left| \Im_{N} \left\{ I_{HD} \right\} \right|^{2}} df - 1 - N_{ENF} \propto E_{r} \quad . \tag{5}$$

Utilizing Rayleigh's energy theorem, it can be shown that  $U_{HD}$  is thereby directly proportional to  $E_r$ , as desired. The factor  $N_{ENF}$  is termed the excess noise factor, and results from the fact that point-by-point normalization is a biased processing procedure, due to the nonlinearity of the division operation. It can be shown that in the case of no signal, for the parameters used in the heterodyne processing shown in this report, the division of two random noise signals results in a value of  $1+N_{ENF}$  of approximately 1.150, as compared to a value of unity for an unbiased processing procedure.  $N_{ENF}$  is strictly a function of the heterodyne SNR, with  $N_{ENF}$  approaching zero at higher SNRs. Since the  $N_{ENF}$  correction is more important at low SNRs than at higher SNRs, a constant value of  $N_{ENF} = 0.150$  corresponding to the no signal case was used in the processing. The details of the heterodyne processing are also given in Appendix C, where the code for the primary heterodyne detection Matlab calculation program DATREDUC\_HD\_X3.m is reproduced.

#### D. Chemometric Theoretical Analysis

The chemometric processing is performed in exactly the same manner for both direct and heterodyne detection, since the computed parameters  $U_{DD}$  and  $U_{HD}$  are both directly proportional to  $E_{\rm r}$ , and therefore to the total transmission of the target gases of interest. The most accurate and least complicated method to isolate the absorption caused by M target gases is, if possible, to perform the same measurement in the absence of the target gases as will be performed with the gases present. The initial step in the analysis procedure is to normalize the receive energy by the transmit energy. The data are then background normalized by a no-gas spectrum, leaving the spectral transmission from the target gases only. For a sequence of N laser lines and M absorbing gases, the set of equations used in the chemometric analysis can be written as

$$T(\lambda_{1}) = \exp(-2\kappa(\lambda_{1}, g_{1}) \operatorname{CL}(g_{1})) \times \exp(-2\kappa(\lambda_{1}, g_{2}) \operatorname{CL}(g_{2})) \times L$$

$$\times \exp(-2\kappa(\lambda_{1}, g_{M}) \operatorname{CL}(g_{M}))$$

$$T(\lambda_{2}) = \exp(-2\kappa(\lambda_{2}, g_{1}) \operatorname{CL}(g_{1})) \times \exp(-2\kappa(\lambda_{2}, g_{2}) \operatorname{CL}(g_{2})) \times L$$

$$\times \exp(-2\kappa(\lambda_{2}, g_{M}) \operatorname{CL}(g_{M}))$$

$$M$$

$$T(\lambda_{N}) = \exp(-2\kappa(\lambda_{N}, g_{1}) \operatorname{CL}(g_{1})) \times \exp(-2\kappa(\lambda_{N}, g_{2}) \operatorname{CL}(g_{2})) \times \cdots$$

$$\times \exp(-2\kappa(\lambda_{N}, g_{M}) \operatorname{CL}(g_{M}))$$

$$(6)$$

where  $T(\lambda_i)$  is the total transmission at wavelength  $\lambda_i$  including the contributions from all of the target gases.

A matrix equation which is linear in the unknowns  $CL(g_i)$  is formed by taking the logarithm of each equation

$$\overline{\mathbf{a}} = \frac{1}{2} \begin{bmatrix}
-\ln(T(\lambda_1)) \\
-\ln(T(\lambda_2)) \\
M \\
-\ln(T(\lambda_N))
\end{bmatrix} = \begin{bmatrix}
\kappa(\lambda_1, g_1) & \kappa(\lambda_1, g_2) & L & \kappa(\lambda_1, g_M) \\
\kappa(\lambda_2, g_1) & \kappa(\lambda_2, g_2) & L & \kappa(\lambda_2, g_M) \\
M & M & M \\
\kappa(\lambda_N, g_1) & \kappa(\lambda_N, g_2) & L & \kappa(\lambda_N, g_M)
\end{bmatrix} \begin{bmatrix}
CL(g_1) \\
CL(g_2) \\
M \\
CL(g_M)
\end{bmatrix} = \mathbf{K} \bullet \overline{\mathbf{c}} \tag{7}$$

Applying singular-value decomposition (SVD) matrix analysis or other techniques to the above equation provides a solution  $\hat{\mathbf{c}}$  for the  $CL(g_i)$ . Some of the advantages of the above chemometric analysis are that all chemical concentrations are solved for simultaneously, and that all of the spectral information available is used in the analysis. These characteristics provide definite improvements over the conventional 2-line DIAL analysis for handling chemicals with overlapping spectral features. Some inaccuracies have been noted for chemicals with overlapping spectral features when using the basic SVD analysis, but it is believed that applying a scheme to de-weight these wavelengths is feasible, and would improve the accuracy of the chemometric results.

#### E. Radiometric Results

The direct detection radiometric results, presented as the ratio of the expected return signal to the actual return signal ( $F_{DD} = \sqrt[6]{DD} / \hat{U}_{DD}$ ) are shown in Figure 22. The results are from experiments conducted on different days using both modelocked and non-modelocked waveforms, and are separated into groups for the four different targets used. Target #1 was the earth berm located at the 4KS site, Target #2 was a highly weathered (2-year exposure) blueboard target at the 4KS site, Target #3 was a moderately weathered (2-month exposure)

blueboard target at the 4KS site, and Target #4 was the 7KS earth berm. Data points that were obvious outliers have been removed from the plot. As seen in the Figure, there is very good agreement between the measured and predicted values (within a factor of 1 - 2.5) for the 4 km and 7 km topographic targets. This agreement level is reasonable, considering that the DIAL measurements had the most emphasis, and the radiometric characterization was therefore not as extensive as had been conducted in past experiments. Previous precise radiometric measurements on the direct detection system conducted in 1998 illustrated that the level of radiometric agreement achievable with the system fully optimized was within a factor of 1 to 1.4.4 The discrepancies seen in Figure 22 for the blueboard targets are most likely caused by inaccuracies in the assumed blueboard target reflectivity. The simulation results used reflectivity values from measurements of the blueboards immediately after they were fabricated, and before being continuously exposed to the outside elements. The blueboard reflectivity is expected to decrease as the target material weathers and blueboard dust particles build up on the surface, and is a reasonable explanation for the results from the blueboard targets. The previous measurements in 1998 were conducted immediately after the blueboard targets had been fabricated and characterized, and both blueboard and berm return signals agreed with predictions within the factor of 1 - 1.4 mentioned previously.

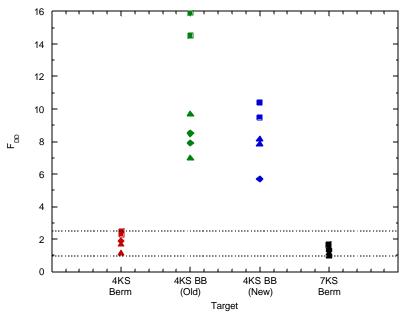


Figure 22. Direct detection radiometric results.

The heterodyne radiometric results are shown in Figure 23. Similarly to the direct detection results, the ratio of expected to measured return signal  $F_{HD} = U_{HD}^{\prime} / \hat{U}_{HD}$  is computed. This ratio is further normalized by the direct detection ratio F<sub>DD</sub>, in order to remove any errors caused by inaccuracies in the assumed reflectivities. Data points that were obvious outliers have been removed from the plot. As seen in the Figure, the heterodyne return signal is within a factor of approximately 6 to 20 of the expected value. The heterodyne return signal simulation includes heterodyne efficiency and signal reduction factors resulting from beam pattern mismatch between the LO (uniform) and return signal (Airy)<sup>5,6</sup>; distortion of the return signal phase front by atmospheric turbulence (assuming a relatively high turbulence level of  $C_n^2 = 10^{-13} \text{ m}^{-2/3}$ )<sup>7</sup>; and loss of signal caused by transmitter beam (pointing) jitter. Factors which were not able to be measured and are not included in the simulation include nonuniformity in the detector quantum efficiency (probably a negligible factor); misalignment of the transmitter footprint and receiver field-of-view (also probably a negligible factor); phase front curvature from misfocusing of the heterodyne receiver telescope (also probably negligible); and angular misalignment of the LO and receiver signal on the detector (possibly a factor of ~2 reduction). It should also be noted that the results of Frehlich and Kavaya [1991] 8 suggest that the coherence loss factor caused by atmospheric turbulence may be significantly worse than that given by Clifford and Wandzura [1981]<sup>7</sup> and used in this paper.

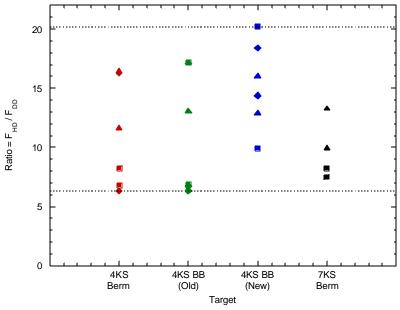


Figure 23. Normalized heterodyne radiometric results.

Overall, the difference between the expected and measured heterodyne signal levels is larger than expected, but not significantly, and could most likely be significantly reduced with a more precise system optimization. The best agreement noted to date between expected and actual return heterodyne signal levels for comparable systems is a factor of  $\sim 4^9$ , with most systems reporting a 5 – 10 dB (factor of 3 – 10) $^{10,11,12,13}$  reduction. With the possible loss factors not included in the analysis of the CROSS system, and the added complexity inherent in a fully wavelength-agile heterodyne system, a reduction factor of 6 – 20 compares favorably with the previous reduction factors from other researchers of 3- 10.

## F. Chemometric Results (Case Studies)

The absorption spectra for  $SF_6$  and  $NH_3$  are shown in Figure 24. The x's indicate the absorption coefficients for the chemicals at the specific wavelengths in the 10R and 10P bands for the  $^{12}C^{16}O_2$  laser isotope being used for the experiments.  $SF_6$  has a broad absorption feature, which will affect most of the 10P laser lines.  $NH_3$  has a much narrower absorption spectrum, and has its only significant absorption on the 10R14 laser line. For the HD/DD DC experiments, only 3-4 of the 10R lines shown on the plot (between ~ 969-982 cm<sup>-1</sup>) were used in the laser sequence.

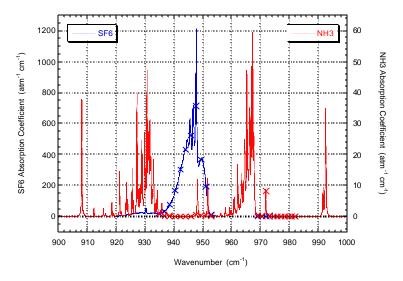


Figure 24. Absorption spectra overlap with <sup>12</sup>C<sup>16</sup>O<sub>2</sub> laser wavelengths for SF<sub>6</sub> and NH<sub>3</sub>.

The results from the HD/DD DC tests using the spread spectrum (modelocked) transmit waveform and the diffuse blueboard target at the 4 km site are shown in Figure 25. The absorption plots for both the direct detection and heterodyne return signals are shown on the left of the Figure. The horizontal axis in these plots corresponds to time, while the vertical axis shows the laser wavelengths transmitted. From sequences 1 to 40, there was no  $SF_6$  present

in the absorption cell. Around sequence 40, a first  $SF_6$  insertion was made, and a second  $SF_6$  insertion was made near sequence 70. The  $SF_6$  absorption signature is seen clearly in both of the absorption plots, although the direct detection plot is cleaner. Rough calculations of the expected single shot SNR give a direct detection  $SNR_{DD} \sim 5$ , resulting from speckle spatial averaging, and a heterodyne single shot  $SNR_{HD} \sim 2.5$ , resulting from approximately 6 effective modes in the transmitted modelocked spectrum. After the DIAL processing techniques are applied, the  $SNR_{S}$  shown in the absorption plots become  $SNR_{DD} \sim 14$  and  $SNR_{HD} \sim 7$ . The graph on the bottom right of the Figure shows the computed concentration-length (CL) products as a function of time for both techniques. The table on the top right summarizes the measured CLs in each of the three reference / insertion regions. The results from the two detection techniques differ by less than 12%, which is reasonably good agreement given the number of uncontrolled variables in the experiment.

The results from the HD/DD DC tests using the spread spectrum (modelocked) transmit waveform and the topographic target at the 7.5 km site are shown in Figure 26. The SF<sub>6</sub> insertion timeline is essentially the same as that described for Figure 25. The SF<sub>6</sub> signature is again evident in both of the absorption plots. The expected single shot SNRs are the same as for the 4 km measurements (SNR<sub>DD</sub>  $\sim$  5 and SNR<sub>HD</sub>  $\sim$  2.5). After the processing techniques are applied, the SNRs become SNR<sub>DD</sub>  $\sim$  14 and SNR<sub>HD</sub>  $\sim$  5, indicating that the direct detection results are similar at both ranges, and the heterodyne results were slightly degraded at the longer range. In this case, the results from the two detection techniques differ by less than 20%, which is still reasonably good agreement.

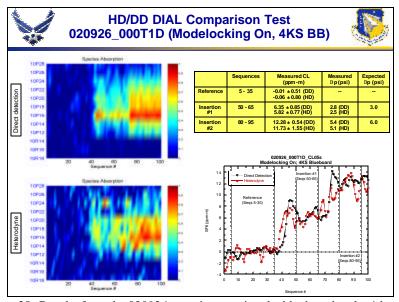


Figure 25. Results from the 020926 experiment using the blueboard at the 4 km site.

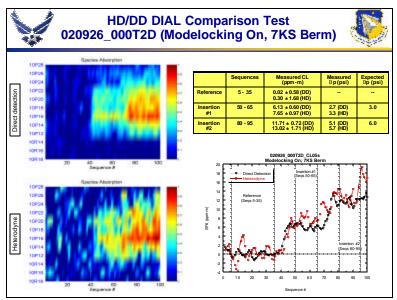


Figure 26. Results from 020926 experiment using topographic returns at the 7.5 km site.

Results from a dual insertion of  $SF_6$  and  $NH_3$  are shown in Figure 27. The  $SF_6$  was inserted around sequence 40, and the  $NH_3$  was inserted near sequence 70. As shown in Figure 24,  $SF_6$  exhibits absorption on most of the 10P laser lines, while  $NH_3$  has significant absorption only at the 10R14 wavelength. The CL values for  $SF_6$  and  $NH_3$  measured with both the direct detection and heterodyne receivers are shown on the plot.

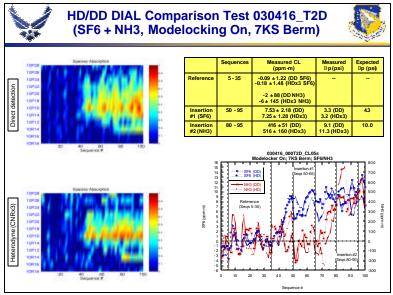


Figure 27. Results from 030416 dual  $SF_6$  and  $NH_3$  experiment using topographic returns at 7.5 km.

Heterodyne and direct detection DIAL results using the blueboard target at a range of 15 km are shown in Figures 28 and 29. The direct detection DIAL results are significantly noisier than at shorter ranges, which is expected since at longer horizontal ranges the direct detection system is signal-limited, and is therefore no longer in the speckle-limited regime. The direct detection signal level for the 030612 data set is extremely low, which causes significant errors in the DIAL intermediate normalization processing algorithm, and appears as the physically incorrect result of the measured absorption being saturated. The heterodyne DIAL results also show some degradation, but not to as great an extent as the direct detection results, which indicates that the heterodyne system is still operating in the speckle-limited regime, as expected.

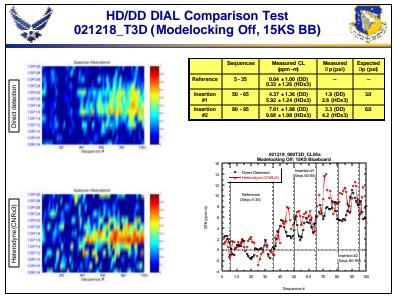


Figure 28. Results from the 021218 experiment using the blueboard at the 15 km site.

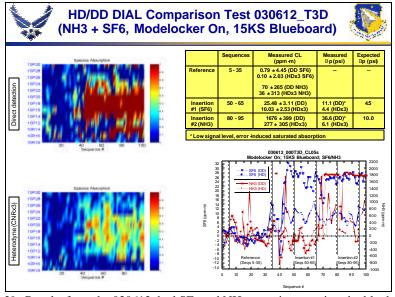


Figure 29. Results from the 030612 dual  $SF_6$  and  $NH_3$  experiment using the blueboard at 15 km.

#### G. Chemometric Results (Compilation and Comparisons)

This section will provide a summary of the DIAL chemometric results for the HD/DD DC experiments. Detailed results for all of the primary HD/DD DC experiments are shown in Appendix B. The expected and measured concentration-length (CL) products from all of the HD/DD DC data sets used in this report are shown in Figure 30. Prior to March 2004 (~ Day #60), the common experiment technique was to begin data collection with no gas in the cell, then add SF<sub>6</sub> approximately 1/3 of the way through the data set, and then add more SF<sub>6</sub> approximately 2/3 of the way through the data set. The initial SF<sub>6</sub> insertion CL measurements are shown in blue in the Figure, with the second SF<sub>6</sub> CL measurements shown in green. After March 2004, the experiment technique was changed to normally have the first insertion with SF<sub>6</sub> (shown in blue), and the second insertion with NH<sub>3</sub> (shown in red). The dashed lines on the plots have no significance, but are shown to more clearly indicate the different gas insertions. To reduce clutter from overlap of the symbols on the plot, measurements from the 4KS blueboards (4KS BB) were shifted left by  $\frac{1}{2}$  day, and measurements from the 7KS berm were shifted right by  $\frac{1}{2}$  day.

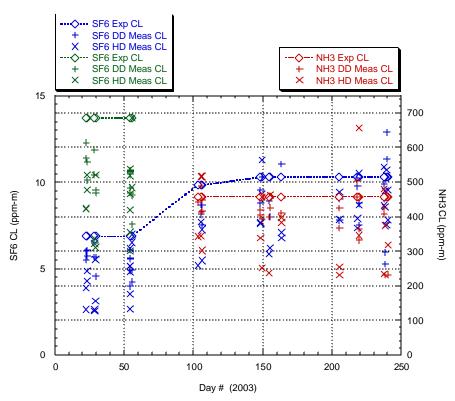


Figure 30. Expected and measured CL values from HD/DD DC experiments.

Although there is a significant amount of scatter in the results shown in Figure 30, a few general conclusions can be drawn. During the time period of these measurements, both the heterodyne and direct detection DIAL systems were being continually improved, both with respect to the equipment, and to the alignment and experimental procedures. This is evidenced by noting that prior to March 2004, the measured CL results were significantly lower than the expected values, and the measured CLs never significantly exceeded the expected values. After March 2004, the measured CLs still tended to be lower than the expected values, but were closer to the expected value, and sometimes exceeded it. This improvement continued until the final measurements made in August of 2004.

It is believed that the measured CL's being consistently lower than expected probably results from a systematic error, possibly from inaccuracies in the gas insertion procedure or from errors in the compensation of the spectral absorption coefficients for the experiment atmospheric pressure and temperature. Since the primary purpose of the HD/DD DC experiment series was to compare heterodyne and direct detection DIAL, relative results were emphasized, and extraordinary efforts were not made to calibrate the system for absolute accuracy. Previous measurements of SF<sub>6</sub>, NH<sub>3</sub>, and Freon R-134A made during ground tests in 19984 with only the LARS direct detection DIAL system showed slightly more accurate DIAL results than achieved with the HD/DD DC direct detection measurements. The more accurate results in 1998 were possible primarily because only a single system and single target were being used, allowing more meticulous alignment and system calibration. The more complex nature of the HD/DD DC experiment reduced the capability to optimize all of the system components simultaneously, and would be expected to result in reduced DIAL measurement accuracy. Even with the slightly reduced accuracy, the comparisons between the heterodyne and direct detection DIAL results are still valid and provide the key information required to analyze and compare the capabilities of the techniques.

To better study the effects of the various system parameters on the DIAL accuracy, the measurements were separated into groups by the experiment and system parameters. A summary of the DIAL results for these related measurements is given in Table 3. The Table separates the measurements by the detection technique used, the target gas, the modelocking configuration, the time period when the measurements were made, the number of individual measurements included in the group, and the average and standard deviation of the measured to expected concentration-length (CL) ratio. It should be noted that even though there were more than 158 individual DIAL measurements made, the compiled grouping results may still not be statistically significant, since there are many parameters which may affect the DIAL measurements, resulting in a small number of similar measurements for each grouping. The DIAL results have a significant amount of scatter, and an empirical decision was made to consider any individual values which fell below 50% or above 150% of the expected CL to be outliers, and to remove these values from the analysis.

Table 3. Summary of DIAL Results

	Table 3. Summary of DIAL Results							
Target	Detection	Target	Mode-	Time	Number of	Measured /		
	Techniqu	Gas	locking	Segment	Measurement	Expected CL		
	e			υ	s	Ratio		
4KS BB	DD	SF6	On	Post–Mar	5	$0.99 \pm 0.15$		
III.S BB	DD	510	Oli	04	3	0.55 ± 0.15		
4KS BB	DD	SF6	Off	Post–Mar	6	$0.93 \pm 0.10$		
4K3 DD	טט	51.0	Oli	()4	U	0.93 ± 0.10		
4IZC DD	IIID	CEC	0			0.77 + 0.17		
4KS BB	HD	SF6	On	Post–Mar	6	$0.77 \pm 0.17$		
ALC DD	IID	an-c	0.00	04		0.70 0.10		
4KS BB	HD	SF6	Off	Post–Mar	5	$0.78 \pm 0.18$		
				04				
7KS Berm	DD	SF6	On	Post–Mar	7	$0.68 \pm 0.24$		
				04				
7KS Berm	DD	SF6	Off	Post–Mar	8	$0.78 \pm 0.28$		
				04				
7KS Berm	HD	SF6	On	Post–Mar	7	$0.87 \pm 0.16$		
				04				
7KS Berm	HD	SF6	Off	Post–Mar	8	$0.76 \pm 0.14$		
				04				
4KS BB	DD	NH3	On	Post–Mar	5	$0.98 \pm 0.06$		
4K3 DD	DD	1413	Oli	04	3	0.70 ± 0.00		
4KS BB	DD	NH3	Off	Post–Mar	5	$0.93 \pm 0.10$		
413 DD	DD	INIIS	Oli	04	3	0.93 ± 0.10		
4KS BB	HD	NH3	On	Post–Mar	4	$0.78 \pm 0.26$		
4N3 DD	пр	NH3	On	Post–Mar 04	4	$0.78 \pm 0.26$		
ALC DD	IID	NHIO	2000		2	0.50 . 0.14		
4KS BB	HD	NH3	Off	Post–Mar	3	$0.59 \pm 0.14$		
				04				
7KS Berm	DD	NH3	On	Post–Mar	5	$0.79 \pm 0.18$		
				04				
7KS Berm	DD	NH3	Off	Post–Mar	7	$0.82 \pm 0.16$		
				04				
7KS Berm	HD	NH3	On	Post–Mar	7	$0.83 \pm 0.20$		
				04				
7KS Berm	HD	NH3	Off	Post–Mar	6	$0.84 \pm 0.34$		
				04				
4KS BB	DD	SF6 (Low)	On	Pre-Mar 04	5	$0.82 \pm 0.08$		
4KS BB	DD	SF6 (Low)	Off	Pre–Mar 04	5	$0.82 \pm 0.08$ $0.80 \pm 0.12$		
		`			5			
4KS BB	HD	SF6 (Low)	On	Pre-Mar 04		$0.55 \pm 0.24$		
4KS BB	HD	SF6 (Low)	Off	Pre–Mar 04	5	$0.59 \pm 0.16$		

4KS BB	DD	SF6 (High)	On	Pre-Mar 04	5	$0.80 \pm 0.09$
4KS BB	DD	SF6 (High)	Off	Pre-Mar 04	5	$0.77 \pm 0.04$
4KS BB	HD	SF6 (High)	On	Pre-Mar 04	5	$0.59 \pm 0.14$
4KS BB	HD	SF6 (High)	Off	Pre-Mar 04	5	$0.61 \pm 0.11$
7KS Berm	DD	SF6 (Low)	On	Pre-Mar 04	3	$0.81 \pm 0.08$
7KS Berm	DD	SF6 (Low)	Off	Pre-Mar 04	3	$0.71 \pm 0.12$
7KS Berm	HD	SF6 (Low)	On	Pre-Mar 04	3	$0.84 \pm 0.15$
7KS Berm	HD	SF6 (Low)	Off	Pre-Mar 04	3	$0.67 \pm 0.25$
7KS Berm	DD	SF6 (High)	On	Pre-Mar 04	3	$0.70 \pm 0.04$
7KS Berm	DD	SF6 (High)	Off	Pre-Mar 04	3	$0.68 \pm 0.13$
7KS Berm	HD	SF6 (High)	On	Pre-Mar 04	3	$0.82 \pm 0.16$
7KS Berm	HD	SF6 (High)	Off	Pre-Mar 04	3	$0.64 \pm 0.17$

The average measured-to-expected CL ratios are shown in Figure 31 for the different data groupings, and the standard deviation of the ratios are shown in Figure 32. The data points are again slightly offset on the x-axis for the different groupings to reduce clutter from overlap of the symbols. As noted previously, definitive conclusions probably should not be drawn from this data because the statistical significance is questionable because of the small number of data points included in each grouping, but some probable conclusions can still be made:

- 1) The pre-March measured CL values are generally lower than those from post-March. As stated previously, this is believed to result from improvements in the system hardware and the experimental alignment and procedures. Because of this effect, it is generally better to rely more on the post-March data to draw conclusions about the effects of the different parameters on the DIAL accuracy.
- 2) The direct detection measurements from the 4KS BB appear to give the most accurate DIAL results, with the closest match to the expected CL value, and the least variability. Referring to Figure 1, this is expected since in the HD/DD DC experiments the direct detection system is expected to outperform the heterodyne system in the speckle-limited regime. This is a result of direct detection spatial averaging providing more speckle mitigation than is achievable with the heterodyne spread spectrum operation in the system configurations used for the HD/DD DC experiments. It should be noted that the amount of speckle mitigation for the heterodyne system could be significantly and easily increased by designing the laser transmitter to include more frequency modes than was possible with the specific BBO laser configuration used in these experiments.
- 3) The direct detection system tends to be in the transition region between speckle- and signal-limited operation at 7 km, while the heterodyne system is still in the speckle-limited region. The DIAL measurement accuracies and variabilities are generally similar for direct detection operation at 7 km, and heterodyne operation at both 4 km and 7 km. This is seen for

both SF<sub>6</sub> and NH<sub>3</sub>, in the post-March data. A possible explanation for this behavior is that the heterodyne system is operating in the speckle-limited regime at both 4 km and 7 km, while the direct detection system is in the speckle-limited regime at 4 km, but is entering the transition region between speckle- and signal-limited operation at 7 km (see Figure 1).

- 4) **Modelocking improves heterodyne DIAL accuracy.** This is most easily seen by noting that the modelocked heterodyne results from 7 km are closer to the expected CL value, and have lower variability than the non-modelocked results. The same results are expected from the 4 km measurements, but the 4 km data does not conclusively support or contradict the expected result.
- 5) **Direct detection results are better with modelocking off.** Since spatial averaging is the primary speckle mitigation technique for direct detection, it is expected that the increased laser power available with non-modelocked operation will provide the best results. The results shown in Figures 31 and 32 generally support this conclusion. A possible reason that not all of the data points demonstrate this result, is that it appears that the system transmit pointing jitter is reduced when using the modelocked pulse train, which improves the DIAL results.

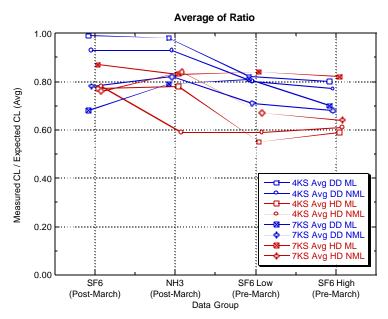


Figure 31. Average measured CL / expected CL ratio.

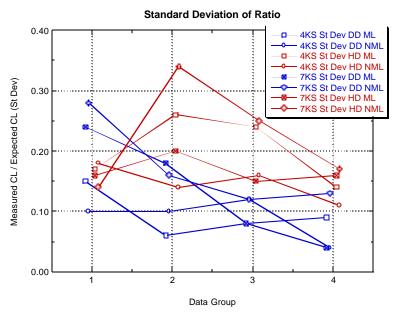


Figure 32. Standard deviation of measured CL  $\!\!/$  expected CL ratio.

## 5. Summary and Conclusions

The HD/DD DC experiments were designed to provide a direct, simultaneous comparison of the radiometric and chemical detection sensitivities of the heterodyne and direct detection receiver techniques. Many parameters affect radiometric and DIAL accuracy, and it is often not clear why measurements differ from the expected results. Numerous unresolved issues exist about the capabilities and characterizations of DIAL systems, especially with respect to systems utilizing heterodyne detection. In order to address some of the major issues, and to provide an empirical comparison of performance when the effects of all individual factors can not be determined, an experiment technique was developed that provided the first direct simultaneous comparisons of heterodyne and direct detection DIAL measurements.

The radiometric results showed that the direct detection return signal was within a factor of 1 to 2.5 of the expected value, while the heterodyne return signal was within a factor of 6 to 20. Previous specialized direct detection radiometric efforts at AFRL/DE had resulted in agreement factors of approximately 1 to 1.4. The premier heterodyne radiometric efforts by other research groups have demonstrated agreement factors of 3 to 10. The level of radiometric agreement achieved in the HD/DD DC experiments is reasonable in comparison with these previous efforts, considering that the primary focus of the experiments was on multiple wavelength DIAL measurements, which significantly increases the system complexity with respect to single wavelength measurements.

A primary issue concerning the accuracy of heterodyne DIAL measurements is the sensitivity of the heterodyne detection process to speckle, which directly affects chemical detection capability. For the HD/DD DC measurements a speckle mitigation technique utilizing a spread spectrum (modelocked) transmit waveform was employed and studied. The heterodyne DIAL results showed slightly higher variability (within a factor of 2, as determined from the minimum detectable absorption level) than the direct detection results, but were much better than the results that would be expected from a heterodyne system not employing a speckle mitigation concept.

The measurements also indicate that the relative DIAL performance of heterodyne detection improves with increasing range in comparison with direct detection, as would be expected. The ability of heterodyne systems to maintain speckle limited performance at ranges where direct detection systems become signal limited allows smaller systems to be used for the same range requirements, and allows a longer standoff range to be achieved with similar size systems.

The primary conclusion of the HD/DD DC experiment series is that heterodyne DIAL is a feasible and demonstrated technique, and has definite utility, especially for long standoff range operation.

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# Appendix A. HD/DD DC Datasets

Table A1. HD/DD DC Datasets

	** 1	P.1	Table A1. HD/L	l	
Date	Used	Filename	Target	Modelocke	Gas / System Configuration
(yymmdd)	in E:			d	
	Figure				
030828		Test	15KS BB	No	No gas cell
030828		Test1a	4KS BB (old)	No	No gas cell
030828		Test1b	4KS BB (old)	Yes	No gas cell
030828		Test1c	4KS berm	No	No gas cell
030828		Test1d	4KS berm	Yes	No gas cell
030828		Test2a	4KS BB (new)	No	No gas cell
030828		Test2b	4KS BB (new)	No	Empty cell / SF6 / NH3
030828		Test2c	4KS BB (new)	Yes	No gas cell
030828		Test2d	4KS BB (new)	Yes	Empty cell / SF6 / NH3
030828		Test3a	7KS berm	No	No gas cell
030828		Test3b	7KS berm	No	Empty cell / SF6 / NH3
030828		Test3c	7KS berm	Yes	No gas cell
030828		Test3d	7KS berm	Yes	Empty cell / SF6 / NH3
030828		Test4a	None	No	System characterization test
030826		Test1a	4KS BB (old)	No	No gas cell
030826		Test1b	4KS BB (old)	Yes	No gas cell
030826		Test1c	4KS berm	No	No gas cell
030826		Test1d	4KS berm	Yes	No gas cell
030826		Test1e	4KS berm	No	No gas cell
030826		Test2a	4KS BB (new)	No	No gas cell
030826		Test2b	4KS BB (new)	No	Empty cell / SF6 / NH3
030826		Test2c	4KS BB (new)	Yes	No gas cell
030826		Test2d	4KS BB (new)	Yes	Empty cell / SF6 / NH3
030826		Test3a	7KS berm	No	No gas cell
030826		Test3b	7KS berm	No	Empty cell / SF6 / NH3
030826		Test3c	7KS berm	Yes	No gas cell
030826		Test3d	7KS berm	Yes	Empty cell / SF6 / NH3
030820		Test1a	4KS BB (old)	No	No gas cell
030820		Test1b	4KS BB (old)	Yes	No gas cell
030820		Test1c	4KS berm	No	No gas cell
030820		Test1d	4KS berm	Yes	No gas cell
030820		Test5a	None	No	System characterization test

030807		Test1a	4KS BB (old)	No	No gas cell
030807	Test1b		4KS BB (old)	Yes	No gas cell
030807	Test1c		4KS berm	No	No gas cell
030807		Test1d	4KS berm	Yes	No gas cell
030807		Test2a	4KS BB (new)	No	No gas cell
030807		Test2b	4KS BB (new)	No	Empty cell / SF6 / NH3
030807		Test2c	4KS BB (new)	Yes	No gas cell
030807		Test2d	4KS BB (new)	Yes	Empty cell / SF6 / NH3
030807		Test3a	7KS berm	No	No gas cell
030807		Test3b	7KS berm	No	Empty cell / SF6 / NH3
030807		Test3c	7KS berm	Yes	No gas cell
030807		Test3d	7KS berm	Yes	Empty cell / SF6 / NH3
030724		Test1a	4KS BB (old)	No	No gas cell
030724		Test1b	4KS BB (old)	Yes	No gas cell
030724		Test1c	4KS berm	No	No gas cell
030724		Test1d	4KS berm	Yes	No gas cell
030724		Test1e	4KS BB (new)	No	No gas cell
030724		Test1f	4KS BB (new)	Yes	No gas cell
030724		Test2a	7KS berm	No	No gas cell
030724		Test2b	7KS berm	No	Empty cell / SF6 / NH3
030724		Test2c	7KS berm	Yes	No gas cell
030724		Test2d	7KS berm	Yes	Empty cell / SF6 / NH3
030612		Test1a	4KS BB (old)	No	No gas cell
030612		Test1b	4KS BB (old)	Yes	No gas cell
030612		Test1c	4KS berm	No	No gas cell
030612		Test1d	4KS berm	Yes	No gas cell
030612		Test1e	4KS BB (new)	No	No gas cell
030612		Test1f	4KS BB (new)	Yes	No gas cell
030612		Test2a	7KS berm	No	No gas cell
030612		Test2b	7KS berm	No	Empty cell / SF6 / NH3
030612		Test2c	7KS berm	Yes	No gas cell
030612		Test2d	7KS berm	Yes	Empty cell / SF6 / NH3
030612		Test3a	15KS BB	No	No gas cell
030612		Test3b	15KS BB	No	Empty cell / SF6 / NH3
030612		Test3c	15KS BB	Yes	No gas cell
030612	29	Test3d	15KS BB	Yes	Empty cell / SF6 / NH3
030604		Test1a	4KS BB (old)	Out	No gas cell
030604		Test1b	4KS berm	Out	No gas cell
030604	1	Test1c	4KS BB (new)	Out	No gas cell

030604         Test2a         7KS berm         Out         No gas cell           030604         Test2b         7KS berm         Out         Empty cell / SF6 / NH3           030529         Test1a         4KS BB (old)         No         No gas cell           030529         Test2b         4KS berm         No         No gas cell           030529         Test2a         4KS berm         No         No gas cell           030529         Test3a         4KS BB (new)         No         No gas cell           030529         Test3a         4KS BB (new)         No         Empty cell / FF6 / NH3           030529         Test3b         4KS BB (new)         Yes         No gas cell           030529         Test3d         4KS BB (new)         Yes         Empty cell / FF6 / NH3           030529         Test4d         7KS berm         No         No gas cell           030529         Test4d         7KS berm         No         Empty cell / FF6 / NH3           030529         Test4d         7KS berm         Yes         No gas cell           030529         Test4d         7KS berm         Yes         Empty cell / FF6 / NH3           030529         Test4d         7KS berm         Yes         E	030604		Test1d	4KS BB (new)	Out	Empty cell / SF6 / NH3
030604         Test2b         7KS berm         Out         Empty cell / SF6 / NH3           030529         Test1a         4KS BB (old)         No         No gas cell           030529         Test2b         4KS BB (old)         Yes         No gas cell           030529         Test2a         4KS berm         No         No gas cell           030529         Test3a         4KS BB (new)         No         No gas cell           030529         Test3a         4KS BB (new)         No         Empty cell / SF6 / NH3           030529         Test3b         4KS BB (new)         Yes         No gas cell           030529         Test3d         4KS BB (new)         Yes         Empty cell / SF6 / NH3           030529         Test4a         7KS berm         No         No gas cell           030529         Test4b         7KS berm         No         Empty cell / SF6 / NH3           030529         Test4c         7KS berm         Yes         Empty cell / SF6 / NH3           030529         Test4d         7KS berm         Yes         Empty cell / SF6 / NH3           030527         Test1a         None         N/A         System char. (HD bias current)           030527         Test1d         None				` ′		* * *
Test1b						Ü
Test1b						
O30529				` '		
O30529				` '		
Test3a						
030529         Test3b         4KS BB (new)         No         Empty cell / SF6 / NH3           030529         Test3c         4KS BB (new)         Yes         No gas cell           030529         Test4d         4KS BB (new)         Yes         Empty cell / SF6 / NH3           030529         Test4b         7KS berm         No         Empty cell / SF6 / NH3           030529         Test4c         7KS berm         Yes         No gas cell           030529         Test4d         7KS berm         Yes         Empty cell / SF6 / NH3           030529         Test4d         7KS berm         Yes         Empty cell / SF6 / NH3           030529         Test1a         None         N/A         System char. (HD bias current)           030527         Test1a         None         N/A         System char. (HD bias current)           030527         Test1d         None         N/A         System char. (HD bias current)           030527         Test1d         4KS BB (new)         No         System characterization           030522         Test1a         4KS BB (new)         No         System characterization           030522         Test1a         4KS BB (new)         No         System characterization           030502 <td></td> <td></td> <td></td> <td></td> <td></td> <td></td>						
030529         Test3c         4KS BB (new)         Yes         No gas cell           030529         Test3d         4KS BB (new)         Yes         Empty cell / SF6 / NH3           030529         Test4a         7KS berm         No         Benpty cell / SF6 / NH3           030529         Test4c         7KS berm         Yes         No gas cell           030529         Test4d         7KS berm         Yes         Empty cell / SF6 / NH3           030529         Test4d         7KS berm         Yes         Empty cell / SF6 / NH3           030529         Test4d         7KS berm         Yes         Empty cell / SF6 / NH3           030527         Test1a         None         N/A         System char. (HD bias current)           030527         Test1b         None         N/A         System char. (HD bias current)           030527         Test1d         None         N/A         System char. (HD bias current)           030522         Test1a         4KS BB (new)         No         System characterization           030522         Test1a         4KS BB (new)         Yes         System characterization           030502         Test1a         4KS BB (new)         No         System characterization           030416 <td></td> <td></td> <td></td> <td>` /</td> <td></td> <td></td>				` /		
Test3d						
030529         Test4b         7KS berm         No         Empty cell / SF6 / NH3           030529         Test4b         7KS berm         No         Empty cell / SF6 / NH3           030529         Test4c         7KS berm         Yes         No gas cell           030529         Test4d         7KS berm         Yes         Empty cell / SF6 / NH3           030527         Test1a         None         N/A         System char. (HD bias current)           030527         Test1c         None         N/A         System char. (HD bias current)           030527         Test1d         None         N/A         System char. (HD bias current)           030527         Test1d         None         N/A         System char. (HD bias current)           030527         Test1d         4KS BB (new)         No         System char. (HD bias current)           030522         Test1a         4KS BB (new)         Yes         System characterization           030502         Test1a         4KS BB (new)         Yes         System characterization           030502         Test1a         4KS BB (new)         Yes         System characterization           030416         Test1a         4KS BB (new)         No         No gas cell				` ′		
030529         Test4b         7KS berm         No         Empty cell / SF6 / NH3           030529         Test4c         7KS berm         Yes         No gas cell           030529         Test4d         7KS berm         Yes         Empty cell / SF6 / NH3           030527         Test1a         None         N/A         System char. (HD bias current)           030527         Test1b         None         N/A         System char. (HD bias current)           030527         Test1d         None         N/A         System char. (HD bias current)           030527         Test1d         None         N/A         System char. (HD bias current)           030527         Test1a         4KS BB (new)         No         System char. (HD bias current)           030522         Test1a         4KS BB (new)         No         System characterization           030522         Test1b         4KS BB (new)         Yes         System characterization           030502         Test1a         4KS BB (new)         No         System characterization           030416         Test1a         4KS BB (new)         No         Empty cell / SF6 / NH3           030416         Test1a         4KS BB (new)         No         Empty cell / SF6 / NH3				` ′	No	* *
030529         Test4c         7KS berm         Yes         No gas cell           030529         Test4d         7KS berm         Yes         Empty cell / SF6 / NH3           030527         Test1a         None         N/A         System char. (HD bias current)           030527         Test1b         None         N/A         System char. (HD bias current)           030527         Test1d         None         N/A         System char. (HD bias current)           030522         Test1a         4KS BB (new)         No         System characterization           030522         Test1b         4KS BB (new)         Yes         System characterization           030502         Test1a         4KS BB (new)         No         System characterization           030502         Test1b         4KS BB (new)         No         System characterization           030416         Test1a         4KS BB (new)         No         No gas cell           030416         Test1a         4KS BB (new)         No         No gas cell           030416         Test1a         4KS BB (new)         No         No gas cell           030416         Test1a         4KS BB (new)         No         No gas cell           030416         Test2a						Š
030529         Test4d         7KS berm         Yes         Empty cell / SF6 / NH3           030527         Test1a         None         N/A         System char. (HD bias current)           030527         Test1b         None         N/A         System char. (HD bias current)           030527         Test1d         None         N/A         System char. (HD bias current)           030522         Test1a         4KS BB (new)         No         System characterization           030522         Test1b         4KS BB (new)         Yes         System characterization           030502         Test1a         4KS BB (new)         No         System characterization           030502         Test1b         4KS BB (new)         No         System characterization           030416         Test1a         4KS BB (new)         No         No gas cell           030416         Test1b         4KS BB (new)         No         Empty cell / SF6 / NH3           030416         Test1a         4KS BB (new)         No         No gas cell           030416         Test1a         4KS BB (new)         No         No gas cell           030416         Test2a         7KS berm         No         No gas cell           030416         T						
030527         Test1a         None         N/A         System char. (HD bias current)           030527         Test1b         None         N/A         System char. (HD bias current)           030527         Test1c         None         N/A         System char. (HD bias current)           030527         Test1d         None         N/A         System char. (HD bias current)           030522         Test1a         4KS BB (new)         No         System characterization           030522         Test1b         4KS BB (new)         Yes         System characterization           030502         Test1a         4KS BB (new)         Yes         System characterization           030416         Test1a         4KS BB (new)         No         No gas cell           030416         Test1b         4KS BB (new)         No         Empty cell / SF6 / NH3           030416         Test1a         4KS BB (new)         No         No gas cell           030416         Test1a         4KS BB (new)         No         No gas cell           030416         Test2a         7KS berm         No         No gas cell           030416         Test2a         7KS berm         No         Empty cell / SF6 / NH3           030416         T	030529			7KS berm	Yes	-
Current   Curr	030527		Test1a	None	N/A	
030527         Test1b         None         N/A         System char. (HD bias current)           030527         Test1c         None         N/A         System char. (HD bias current)           030527         Test1d         None         N/A         System char. (HD bias current)           030522         Test1a         4KS BB (new)         No         System characterization           030522         Test1b         4KS BB (new)         Yes         System characterization           030502         Test1a         4KS BB (new)         No         System characterization           030502         Test1b         4KS BB (new)         Yes         System characterization           030416         Test1a         4KS BB (new)         No         No gas cell           030416         Test1b         4KS BB (new)         No         Empty cell / SF6 / NH3           030416         Test1a         4KS BB (new)         Yes         Empty cell / SF6 / NH3           030416         Test2a         7KS berm         No         No gas cell           030416         Test2a         7KS berm         No         Empty cell / SF6 / NH3           030416         Test2a         7KS berm         No         Empty cell / SF6 / NH3           030416	030527		restra	rtone	14/11	
Current   Current   Current   Current	030527		Test1b	None	N/A	,
Current   Current   Current   O30527						· `
030527         Test1d         None         N/A         System char. (HD bias current)           030522         Test1a         4KS BB (new)         No         System characterization           030522         Test1b         4KS BB (new)         Yes         System characterization           030502         Test1a         4KS BB (new)         No         System characterization           030502         Test1b         4KS BB (new)         Yes         System characterization           030416         Test1a         4KS BB (new)         No         No gas cell           030416         Test1b         4KS BB (new)         No         Empty cell / SF6 / NH3           030416         Test1a         4KS BB (new)         No         No gas cell           030416         Test1d         4KS BB (new)         Yes         Empty cell / SF6 / NH3           030416         Test2a         7KS berm         No         No gas cell           030416         Test2b         7KS berm         No         Empty cell / SF6 / NH3           030416         Test2c         7KS berm         Yes         No gas cell           030416         Test2c         7KS berm         Yes         Empty cell / SF6 / NH3           030416         Test2d </td <td>030527</td> <td></td> <td>Test1c</td> <td>None</td> <td>N/A</td> <td>System char. (HD bias</td>	030527		Test1c	None	N/A	System char. (HD bias
030522         Test1a         4KS BB (new)         No         System characterization           030522         Test1b         4KS BB (new)         Yes         System characterization           030502         Test1a         4KS BB (new)         No         System characterization           030502         Test1b         4KS BB (new)         No         No gas cell           030416         Test1a         4KS BB (new)         No         Empty cell / SF6 / NH3           030416         Test1c         4KS BB (new)         No         No gas cell           030416         Test1a         4KS BB (new)         No         No gas cell           030416         Test1a         4KS BB (new)         Yes         Empty cell / SF6 / NH3           030416         Test2a         7KS berm         No         No gas cell           030416         Test2b         7KS berm         No         Empty cell / SF6 / NH3           030416         Test2c         7KS berm         Yes         No gas cell           030416         Test2c         7KS berm         Yes         Empty cell / SF6 / NH3           030416         Test2c         7KS berm         Yes         Empty cell / SF6 / NH3           030416         Test1a         4						current)
030522         Test1a         4KS BB (new)         No         System characterization           030522         Test1b         4KS BB (new)         Yes         System characterization           030502         Test1a         4KS BB (new)         No         System characterization           030502         Test1b         4KS BB (new)         Yes         System characterization           030416         Test1a         4KS BB (new)         No         No gas cell           030416         Test1b         4KS BB (new)         Yes         No gas cell           030416         Test1aa         4KS BB (new)         No         No gas cell           030416         Test1d         4KS BB (new)         Yes         Empty cell / SF6 / NH3           030416         Test2a         7KS berm         No         No gas cell           030416         Test2b         7KS berm         No         Empty cell / SF6 / NH3           030416         Test2c         7KS berm         Yes         No gas cell           030416         Test2c         7KS berm         Yes         Empty cell / SF6 / NH3           030416         Test2d         7KS berm         Yes         Empty cell / SF6 / NH3           030416         Test1a         <	030527		Test1d	None	N/A	System char. (HD bias
030522         Test1b         4KS BB (new)         Yes         System characterization           030502         Test1a         4KS BB (new)         No         System characterization           030502         Test1b         4KS BB (new)         Yes         System characterization           030416         Test1a         4KS BB (new)         No         No gas cell           030416         Test1b         4KS BB (new)         No         Empty cell / SF6 / NH3           030416         Test1aa         4KS BB (new)         No         No gas cell           030416         Test1d         4KS BB (new)         Yes         Empty cell / SF6 / NH3           030416         Test2a         7KS berm         No         No gas cell           030416         Test2b         7KS berm         No         Empty cell / SF6 / NH3           030416         Test2c         7KS berm         Yes         No gas cell           030416         Test2d         7KS berm         Yes         Empty cell / SF6 / NH3           030416         Test2d         7KS berm         Yes         Empty cell / SF6 / NH3           030416         Test1a         4KS BB (old)         No         No gas cell           030415         Test1b <td< td=""><td></td><td></td><td></td><td></td><td></td><td>current)</td></td<>						current)
030502         Test1a         4KS BB (new)         No         System characterization           030502         Test1b         4KS BB (new)         Yes         System characterization           030416         Test1a         4KS BB (new)         No         No gas cell           030416         Test1b         4KS BB (new)         No         Empty cell / SF6 / NH3           030416         Test1a         4KS BB (new)         No         No gas cell           030416         Test1a         4KS BB (new)         Yes         Empty cell / SF6 / NH3           030416         Test2a         7KS berm         No         No gas cell           030416         Test2b         7KS berm         No         Empty cell / SF6 / NH3           030416         Test2b         7KS berm         Yes         No gas cell           030416         Test2c         7KS berm         Yes         Empty cell / SF6 / NH3           030416         Test2d         7KS berm         Yes         Empty cell / SF6 / NH3           030416         Test1a         4KS BB (old)         No         No gas cell	030522		Test1a	4KS BB (new)	No	System characterization
030502         Test1b         4KS BB (new)         Yes         System characterization           030416         Test1a         4KS BB (new)         No         No gas cell           030416         Test1b         4KS BB (new)         No         Empty cell / SF6 / NH3           030416         Test1a         4KS BB (new)         Yes         No gas cell           030416         Test1a         4KS BB (new)         Yes         Empty cell / SF6 / NH3           030416         Test2a         7KS berm         No         No gas cell           030416         Test2b         7KS berm         No         Empty cell / SF6 / NH3           030416         Test2c         7KS berm         Yes         No gas cell           030416         Test2c         7KS berm         Yes         Empty cell / SF6 / NH3           030416         Test2d         7KS berm         Yes         Empty cell / SF6 / NH3           030416         Test1a         4KS BB (old)         No         No gas cell           030415         Test1b         4KS BB (old)         Yes         No gas cell	030522		Test1b	4KS BB (new)	Yes	System characterization
030416         Test1a         4KS BB (new)         No         No gas cell           030416         Test1b         4KS BB (new)         No         Empty cell / SF6 / NH3           030416         Test1c         4KS BB (new)         Yes         No gas cell           030416         Test1aa         4KS BB (new)         Yes         Empty cell / SF6 / NH3           030416         Test2a         7KS berm         No         No gas cell           030416         Test2b         7KS berm         No         Empty cell / SF6 / NH3           030416         Test2b         7KS berm         Yes         No gas cell           030416         Test2c         7KS berm         Yes         Empty cell / SF6 / NH3           030416         27         Test2d         7KS berm         Yes         Empty cell / SF6 / NH3           030415         Test1a         4KS BB (old)         No         No gas cell           030415         Test1b         4KS BB (old)         Yes         No gas cell	030502		Test1a	4KS BB (new)	No	System characterization
030416         Test1b         4KS BB (new)         No         Empty cell / SF6 / NH3           030416         Test1c         4KS BB (new)         Yes         No gas cell           030416         Test1aa         4KS BB (new)         No         No gas cell           030416         Test1d         4KS BB (new)         Yes         Empty cell / SF6 / NH3           030416         Test2a         7KS berm         No         No gas cell           030416         Test2b         7KS berm         Yes         No gas cell           030416         Test2c         7KS berm         Yes         No gas cell           030416         27         Test2d         7KS berm         Yes         Empty cell / SF6 / NH3           030415         Test1a         4KS BB (old)         No         No gas cell           030415         Test1b         4KS BB (old)         Yes         No gas cell	030502		Test1b	4KS BB (new)	Yes	System characterization
030416         Test1c         4KS BB (new)         Yes         No gas cell           030416         Test1aa         4KS BB (new)         No         No gas cell           030416         Test1d         4KS BB (new)         Yes         Empty cell / SF6 / NH3           030416         Test2a         7KS berm         No         No gas cell           030416         Test2b         7KS berm         No         Empty cell / SF6 / NH3           030416         Test2c         7KS berm         Yes         No gas cell           030416         27         Test2d         7KS berm         Yes         Empty cell / SF6 / NH3           030415         Test1a         4KS BB (old)         No         No gas cell           030415         Test1b         4KS BB (old)         Yes         No gas cell	030416		Test1a	4KS BB (new)	No	No gas cell
030416         Test1aa         4KS BB (new)         No         No gas cell           030416         Test1d         4KS BB (new)         Yes         Empty cell / SF6 / NH3           030416         Test2a         7KS berm         No         No gas cell           030416         Test2b         7KS berm         No         Empty cell / SF6 / NH3           030416         Test2c         7KS berm         Yes         No gas cell           030416         27         Test2d         7KS berm         Yes         Empty cell / SF6 / NH3           030415         Test1a         4KS BB (old)         No         No gas cell           030415         Test1b         4KS BB (old)         Yes         No gas cell	030416		Test1b	4KS BB (new)	No	Empty cell / SF6 / NH3
030416         Test1d         4KS BB (new)         Yes         Empty cell / SF6 / NH3           030416         Test2a         7KS berm         No         No gas cell           030416         Test2b         7KS berm         No         Empty cell / SF6 / NH3           030416         Test2c         7KS berm         Yes         No gas cell           030416         27         Test2d         7KS berm         Yes         Empty cell / SF6 / NH3           030415         Test1a         4KS BB (old)         No         No gas cell           030415         Test1b         4KS BB (old)         Yes         No gas cell	030416		Test1c	4KS BB (new)	Yes	No gas cell
030416         Test2a         7KS berm         No         No gas cell           030416         Test2b         7KS berm         No         Empty cell / SF6 / NH3           030416         Test2c         7KS berm         Yes         No gas cell           030416         27         Test2d         7KS berm         Yes         Empty cell / SF6 / NH3           030415         Test1a         4KS BB (old)         No         No gas cell           030415         Test1b         4KS BB (old)         Yes         No gas cell	030416		Test1aa	4KS BB (new)	No	No gas cell
030416         Test2b         7KS berm         No         Empty cell / SF6 / NH3           030416         Test2c         7KS berm         Yes         No gas cell           030416         27         Test2d         7KS berm         Yes         Empty cell / SF6 / NH3           030415         Test1a         4KS BB (old)         No         No gas cell           030415         Test1b         4KS BB (old)         Yes         No gas cell	030416		Test1d	4KS BB (new)	Yes	Empty cell / SF6 / NH3
030416         Test2c         7KS berm         Yes         No gas cell           030416         27         Test2d         7KS berm         Yes         Empty cell / SF6 / NH3           030415         Test1a         4KS BB (old)         No         No gas cell           030415         Test1b         4KS BB (old)         Yes         No gas cell	030416		Test2a	7KS berm	No	No gas cell
030416         27         Test2d         7KS berm         Yes         Empty cell / SF6 / NH3           030415         Test1a         4KS BB (old)         No         No gas cell           030415         Test1b         4KS BB (old)         Yes         No gas cell	030416		Test2b	7KS berm	No	Empty cell / SF6 / NH3
030415         Test1a         4KS BB (old)         No         No gas cell           030415         Test1b         4KS BB (old)         Yes         No gas cell	030416		Test2c	7KS berm	Yes	No gas cell
030415 Test1b 4KS BB (old) Yes No gas cell	030416	27	Test2d	7KS berm	Yes	Empty cell / SF6 / NH3
	030415		Test1a	4KS BB (old)	No	No gas cell
030/15 Test c /KS RR (new) Vac No gas call	030415		Test1b	4KS BB (old)	Yes	No gas cell
050-15   105tic   4K5 DD (iicw)   165   100 gds Cell	030415		Test1c	4KS BB (new)	Yes	No gas cell

030415	Test1d	4KS BB (new)	Yes	Empty cell / SF6 / NH3
030415	Test1e	4KS BB (new)	No	No gas cell
030415	Test1f	4KS BB (new)	No	Empty cell / SF6 / NH3
030401	Test1a	4KS BB (old)	No	No gas cell
030401	Test1b	4KS BB (old)	No	Empty cell / SF6 / SF6
030401	Test1c	4KS BB (old)	Yes	No gas cell
030401	Test1d	4KS BB (old)	Yes	Empty cell / SF6 / SF6
030401	Test1e	4KS berm	No	No gas cell
030401	Test1f	4KS berm	Yes	No gas cell
030401	Test2a	7KS berm	No	No gas cell
030401	Test2b	7KS berm	No	Empty cell / SF6 / SF6
030401	Test2c	7KS berm	Yes	No gas cell
030401	Test2d	7KS berm	Yes	Empty cell / SF6 / SF6
030401	Test3a	6KS CC	No	No gas cell
030401	Test3b	6KS CC	No	Empty cell / SF6 / SF6
030401	Test3c	6KS CC	Yes	No gas cell
030401	Test3d	6KS CC	Yes	Empty cell / SF6 / SF6
030321	Test1a	6KS CC	No	No gas cell
030321	Test1b	6KS CC	Yes	No gas cell
030321	Test1c	6KS CC	Yes	No gas cell
030321	Test2a	4KS BB (old)	No	No gas cell
030224	Test1a	4KS BB (old)	No	No gas cell
030224	Test1b	4KS BB (old)	No	Empty cell / SF6 / SF6
030224	Test1c	4KS BB (old)	Yes	No gas cell
030224	Test1d	4KS BB (old)	Yes	Empty cell / SF6 / SF6
030224	Test2a	4KS BB (old)	No	No gas cell
030224	Test2b	4KS BB (old)	No	Empty cell / SF6 / SF6
030224	Test2c	4KS BB (old)	Yes	No gas cell
030224	Test2d	4KS BB (old)	Yes	Empty cell / SF6 / SF6
030224	Test3a	4KS BB (old)	No	No gas cell
030224	Test3b	4KS BB (old)	No	Empty cell / SF6 / SF6
030224	Test3c	4KS BB (old)	Yes	No gas cell
030224	Test3d	4KS BB (old)	Yes	Empty cell / SF6 / SF6
030224	Test4a	7KS berm	No	No gas cell
030224	Test4b	7KS berm	No	Empty cell / SF6 / SF6
030224	Test4c	7KS berm	Yes	No gas cell
030224	Test4d	7KS berm	Yes	Empty cell / SF6 / SF6
030204	Test1a	4KS BB (old)	No	Empty cell / SF6 / SF6
030204	Test1b	4KS BB (old)	Yes	Empty cell / SF6 / SF6

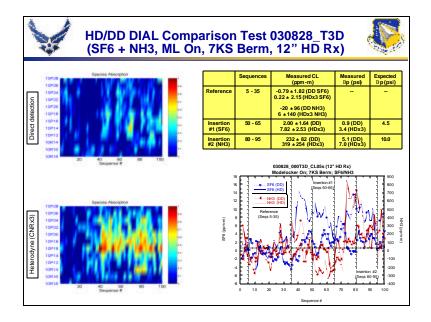
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030204		Test1c	4KS BB (old)	No	Empty cell / SF6 / SF6
030204		Test1d	4KS BB (old)	Yes	Empty cell / SF6 / SF6
030204		Test1e	4KS BB (old)	No	No gas cell
030204		Test1f	4KS BB (old)	Yes	No gas cell
030204		Test2a	7KS berm	No	No gas cell
030204		Test2b	7KS berm	No	Empty cell / SF6 / SF6
030204		Test2c	7KS berm	Yes	Empty cell / SF6 / SF6
030204		Test2d	7KS berm	Yes	No gas cell
030129		Test1a	4KS BB (old)	No	No gas cell
030129		Test1b	4KS BB (old)	No	Empty cell / SF6 / SF6
030129		Test1c	4KS BB (old)	Yes	No gas cell
030129		Test1d	4KS BB (old)	Yes	Empty cell / SF6 / SF6
030129		Test2a	7KS berm	No	No gas cell
030129		Test2b	7KS berm	No	Empty cell / SF6 / SF6
030129		Test2c	7KS berm	Yes	No gas cell
030129		Test2d	7KS berm	Yes	Empty cell / SF6 / SF6
030123		Test1a	4KS BB (old)	No	No gas cell
030123		Test1b	4KS BB (old)	No	Empty cell / SF6 / SF6
030123		Test1c	4KS BB (old)	Yes	No gas cell
030123		Test1d	4KS BB (old)	Yes	Empty cell / SF6 / SF6
030123		Test2a	7KS berm	No	No gas cell
030123		Test2b	7KS berm	No	Empty cell / SF6 / SF6
030123		Test2c	7KS berm	Yes	No gas cell
030123		Test2d	7KS berm	Yes	Empty cell / SF6 / SF6
021218		Test1a	4KS BB (old)	No	No gas cell
021218		Test1b	4KS BB (old)	No	Empty cell / SF6 / SF6
021218		Test1c	4KS BB (old)	Yes	No gas cell
021218		Test1d	4KS BB (old)	Yes	Empty cell / SF6 / SF6
021218		Test2a	7KS berm	No	No gas cell
021218		Test2b	7KS berm	No	Empty cell / SF6 / SF6
021218		Test2c	7KS berm	Yes	No gas cell
021218		Test2d	7KS berm	Yes	Empty cell / SF6 / SF6
021218		Test3a	15KS BB	No	No gas cell
021218		Test3b	15KS BB	No	Empty cell / SF6 / SF6
021218		Test3c	15KS BB	No	No gas cell
021218	28	Test3d	15KS BB	No	Empty cell / SF6 / SF6
021218		Test3e	15KS BB	Yes	No gas cell
021218		Test3f	15KS BB	Yes	Empty cell / SF6 / SF6
021217		Test1a	15KS BB	No	No gas cell

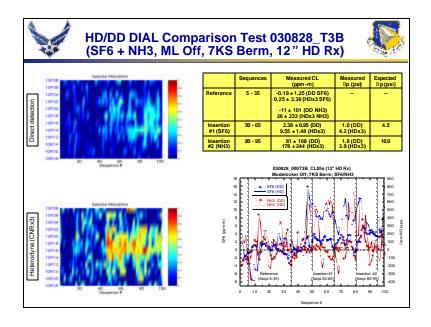
				•	
021217		Test2a	4KS BB (old)	No	No gas cell
021217		Test2b	4KS BB (old)	No	Empty cell / SF6 / SF6
021217		Test2c	4KS BB (old)	Yes	No gas cell
021217		Test2d	4KS BB (old)	Yes	Empty cell / SF6 / SF6
020926		Test1a	4KS BB (old)	No	Empty cell / SF6 / SF6
020926		Test1b	4KS BB (old)	No	No gas cell
020926		Test1c	4KS BB (old)	Yes	No gas cell
020926	25	Test1d	4KS BB (old)	Yes	Empty cell / SF6 / SF6
020926		Test1e	4KS BB (old)	Yes	No gas cell
020926		Test1f	4KS BB (old)	Yes	Empty cell / SF6 / SF6
020926		Test2a	7KS berm	Yes	No gas cell
020926		Test2b	7KS berm	Yes	Empty cell / SF6 / SF6
020926		Test2c	7KS berm	Yes	No gas cell
020926	26	Test2d	7KS berm	Yes	Empty cell / SF6 / SF6
020926		Test2e	7KS berm	No	No gas cell
020926		Test2f	7KS berm	No	Empty cell / SF6 / SF6
020916		Test1a	4KS BB (old)	No	Empty cell / SF6 / SF6
020916		Test1b	4KS BB (old)	No	No gas cell
020916		Test1c	4KS BB (old)	Yes	No gas cell
020916		Test1d	4KS BB (old)	Yes	Empty cell / SF6 / SF6
020916		Test2a	7KS berm	No	No gas cell
020916		Test2b	7KS berm	No	Empty cell / SF6 / SF6
020916		Test2c	7KS berm	Yes	No gas cell
020916		Test2d	7KS berm	Yes	Empty cell / SF6 / SF6
020821		Test1a	4KS BB (old)	Yes	Empty cell / SF6 / SF6
020821		Test1b	4KS BB (old)	Yes	No gas cell
020821		Test1c	4KS BB (old)	No	No gas cell
020821		Test1d	4KS BB (old)	No	Empty cell / SF6 / SF6
020821		Test2a	7KS berm	Yes	No gas cell
020821		Test2b	7KS berm	Yes	Empty cell / SF6 / SF6
020821		Test2c	7KS berm	No	No gas cell
020821		Test2d	7KS berm	No	Empty cell / SF6 / SF6
020806		Test1a	4KS BB (old)	Yes	No gas cell
020806		Test1b	4KS BB (old)	Yes	Empty cell / SF6 / SF6
020806		Test1c	4KS BB (old)	No	No gas cell
020806		Test1d	4KS BB (old)	No	Empty cell / SF6 / SF6
020717		Test1a	4KS BB (old)	No	No gas cell, 10P20 only
020717		Test1c	4KS BB (old)	No	No gas cell, 10P20 only
020717		Test1d	4KS BB (old)	Yes	No gas cell, 10P20 only

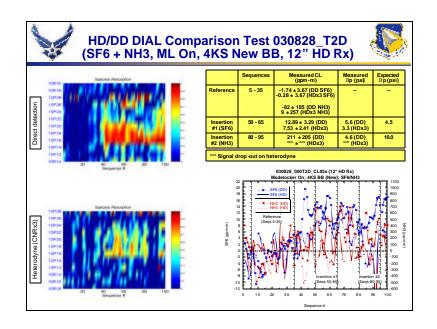
020717	Test2a	4KS BB (old)	No	Empty cell / SF6 / SF6
020717	Test2b	4KS BB (old)	No	No gas cell
020717	Test2c	4KS BB (old)	Yes	No gas cell
020717	Test2d	4KS BB (old)	Yes	Empty cell / SF6 / SF6
020717	Test3a	7KS berm	No	No gas cell, 10P20 only
020717	Test3b	7KS berm	Yes	No gas cell, 10P20 only
020717	Test4a	7KS berm	No	No gas cell
020717	Test4b	7KS berm	Yes	No gas cell
020711	Test1a	4KS BB (old)	No	No gas cell, 10P20 only
020711	Test1b	4KS BB (old)	Yes	No gas cell, 10P20 only
020711	Test2a	4KS BB (old)	No	Empty cell / SF6 / SF6
020711	Test2b	4KS BB (old)	No	No gas cell
020711	Test2c	4KS BB (old)	Yes	No gas cell
020711	Test2d	4KS BB (old)	Yes	Empty cell / SF6 / SF6
020711	Test3a	None	No	System characterization test
020711	Test3b	None	Yes	System characterization test
020710	Test1a	4KS BB (old)	No	No gas cell, 10P20 only
020710	Test2a	4KS BB (old)	Yes	No gas cell, 10P20 only
020710	Test3a	4KS BB (old)	No	Empty cell / SF6 / SF6
020710	Test3b	4KS BB (old)	Yes	Empty cell / SF6 / SF6
020710	Test3c	4KS BB (old)	No	No gas cell
020710	Test3d	4KS BB (old)	Yes	No gas cell
020710	Test4a	7KS berm	No	No gas cell
020710	Test4b	7KS berm	Yes	No gas cell
020710	Test4c	7KS berm	No	Empty cell / SF6 / SF6
020710	Test4d	7KS berm	Yes	Empty cell / SF6 / SF6
020703	Test1a	4KS BB (old)	No	No gas cell, 10P20 only
020703	Test1b	4KS BB (old)	Yes	No gas cell, 10P20 only
020703	Test2a	4KS BB (old)	No	Empty cell / SF6 / SF6
020703	Test2b	4KS BB (old)	No	Empty cell / SF6 / SF6
020703	Test2c	4KS BB (old)	No	No gas cell
020703	Test2d	4KS BB (old)	Yes	Empty cell / SF6 / SF6
020703	Test3a	7KS berm	No	No gas cell
020703	Test3b	7KS berm	Yes	No gas cell
020703	Test3c	7KS berm	No	Empty cell / SF6 / SF6
020703	Test3d	7KS berm	Yes	Empty cell / SF6 / SF6
020703	Test4a	7KS berm	No	No gas cell
020703	Test4b	7KS berm	Yes	No gas cell
020529	Test1a	4KS berm	Yes	Empty cell / SF6 / SF6

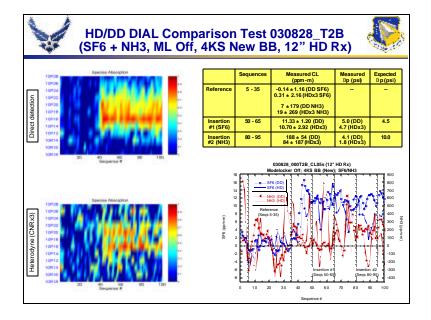
020529	Test1b	4KS berm	Yes	Empty cell / SF6 / SF6
020513	Test1	4KS berm	Yes	Empty cell / SF6 / SF6
020513	Test2	7KS berm	Yes	Empty cell / SF6 / SF6
020513	Test3	7KS berm	Yes	Empty cell / SF6 / SF6
020507	Test1	4KS BB (old)	Yes	Empty cell / SF6 / SF6
020507	Test2	7KS berm	Yes	Empty cell / SF6 / SF6
020506	Test1	4KS BB (old)	Yes	No gas cell
020506	Test2	4KS BB (old)	Yes	Empty cell / SF6 / SF6
020506	Test3	7KS berm	Yes	SF6 (steady state)
020506	Test4	4KS BB (old)	Yes	SF6 (steady state)
020506	Test5	4KS BB (old)	Yes	No gas cell
020506	Test7	4KS BB (old)	Yes	No gas cell

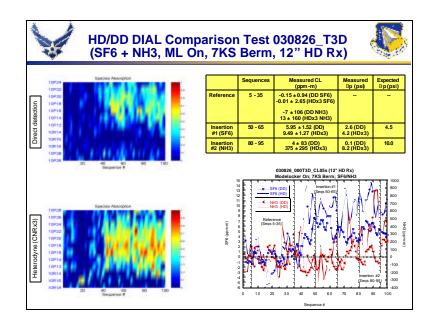
## Appendix B. HD/DD DC DIAL Results

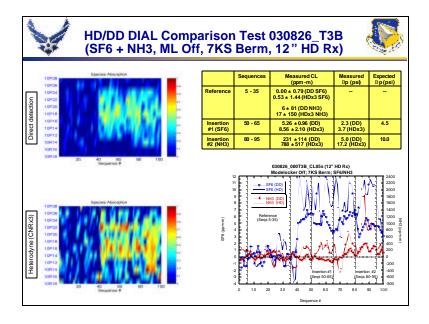


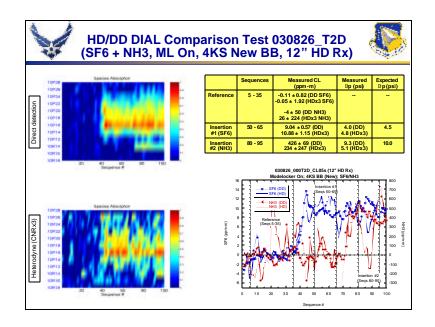


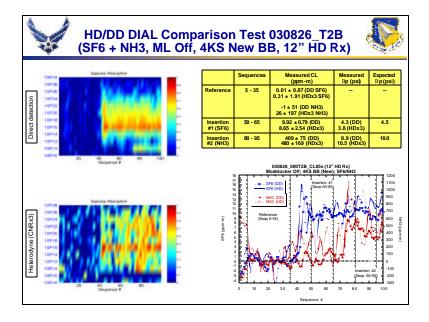


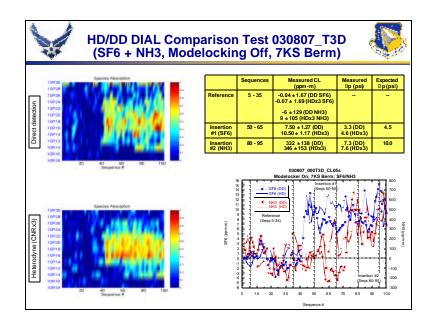


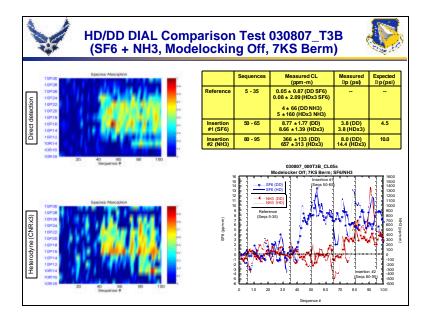


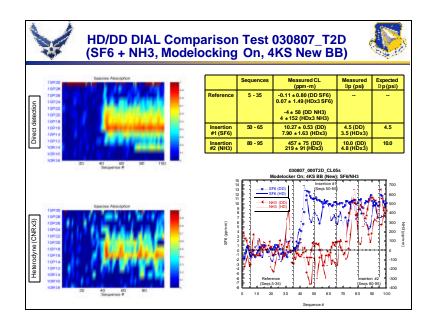


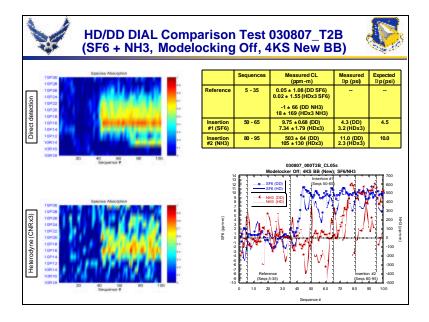


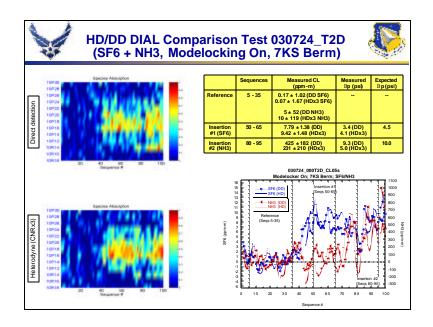


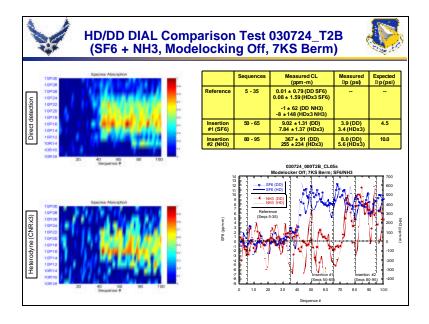


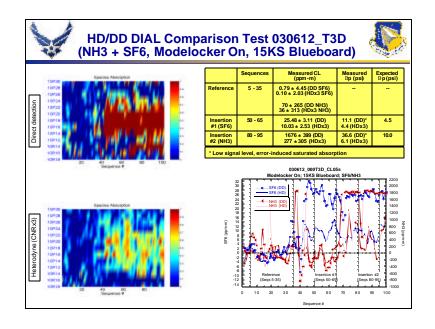


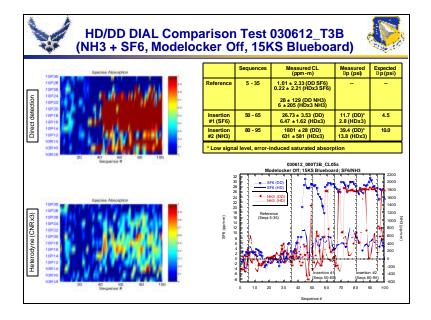


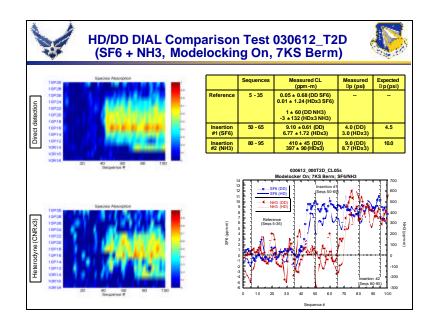


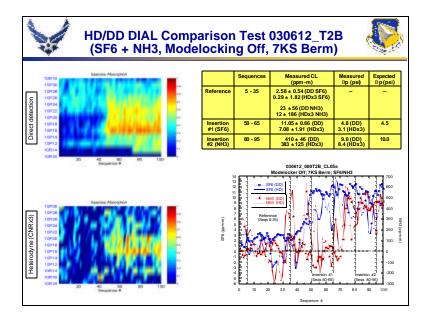


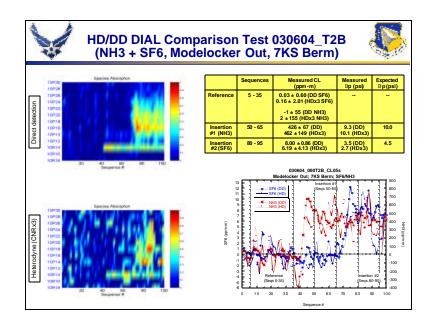


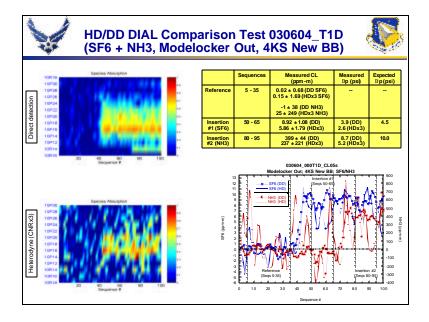


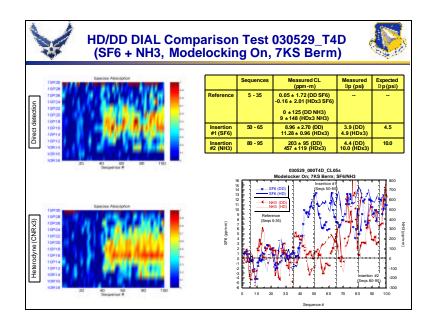


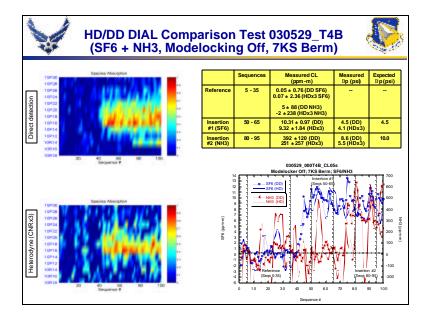


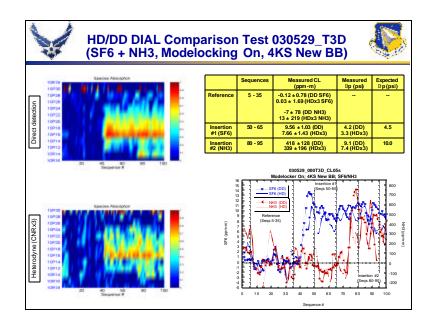


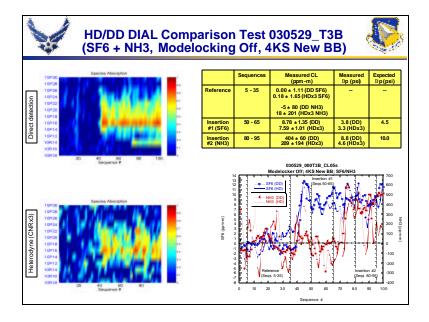


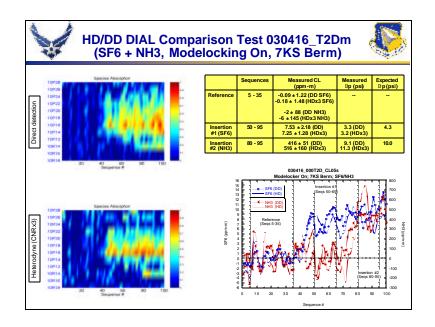


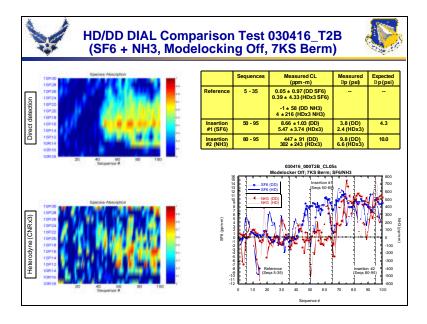


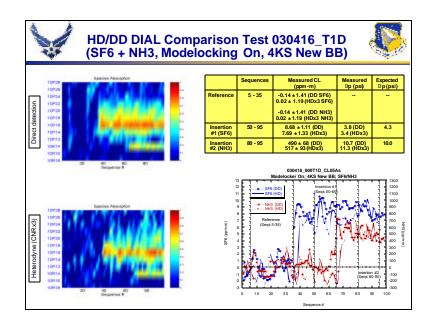


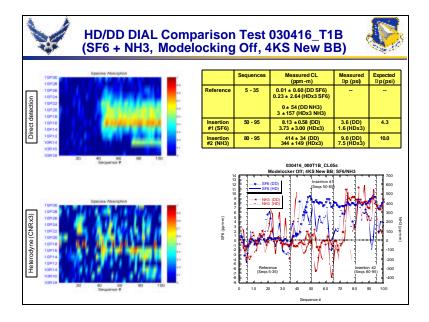


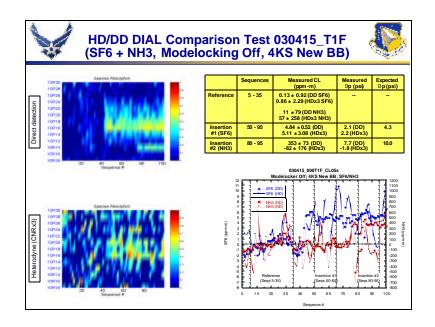


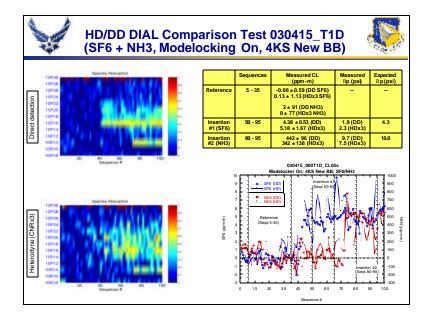


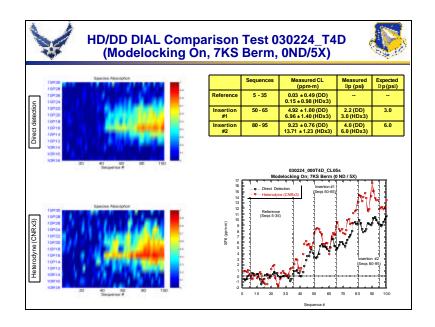


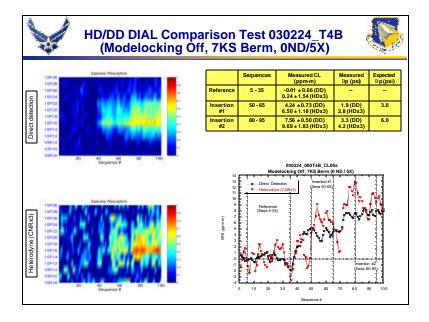


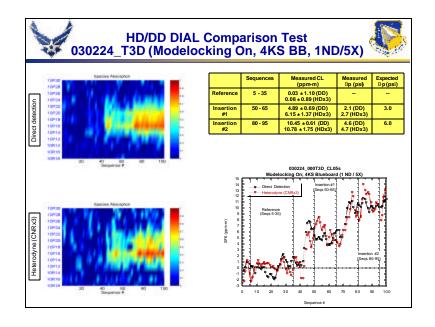


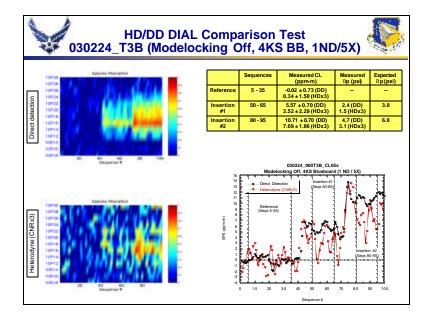


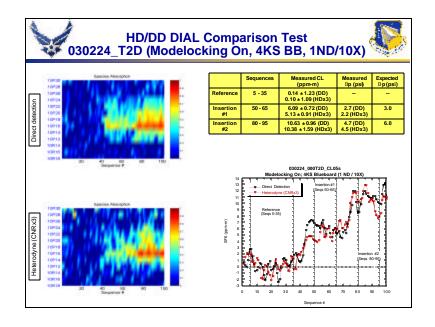


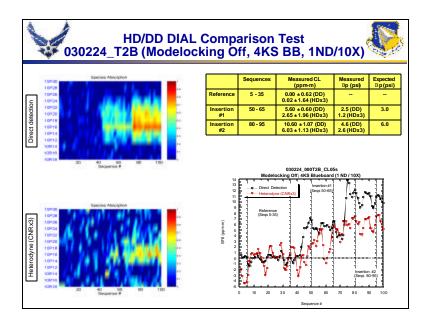


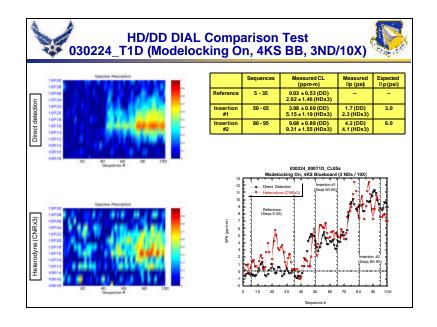


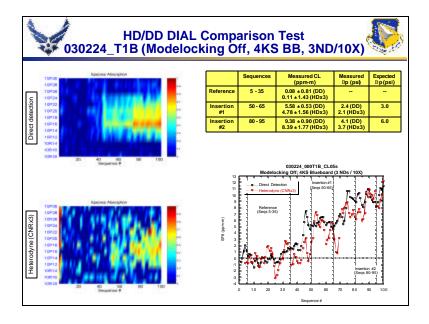


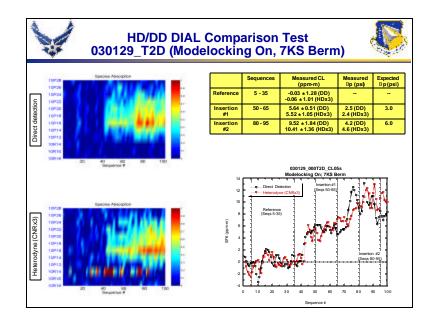


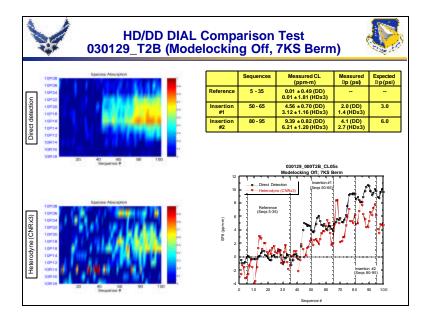


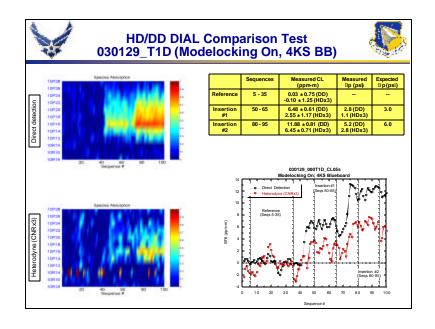


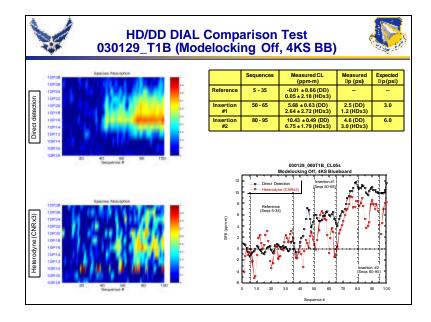


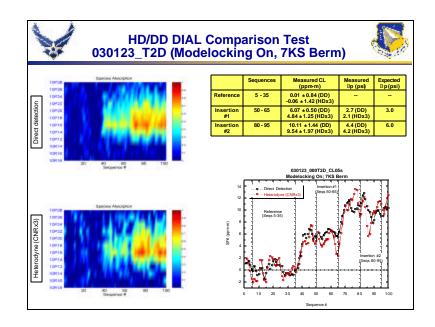


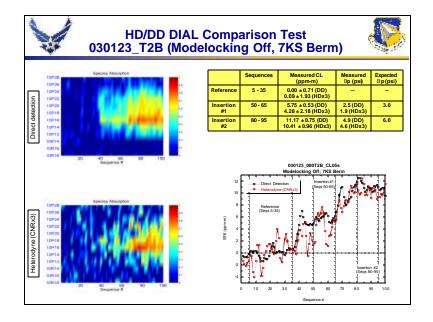


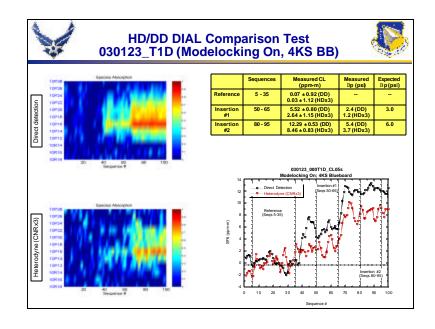


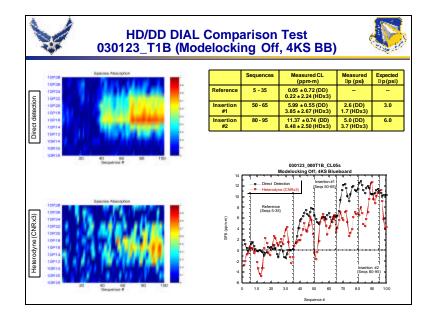


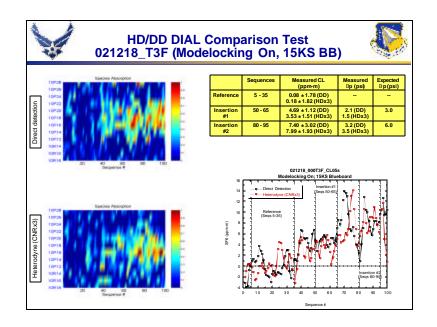


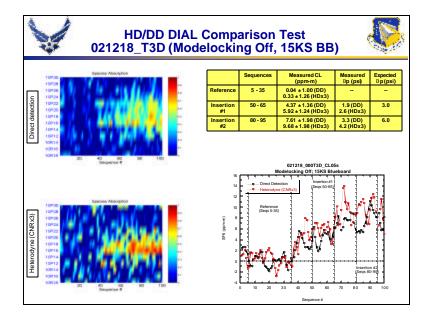


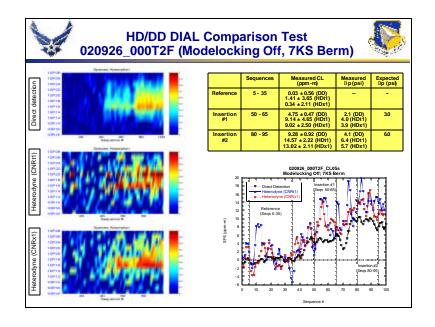


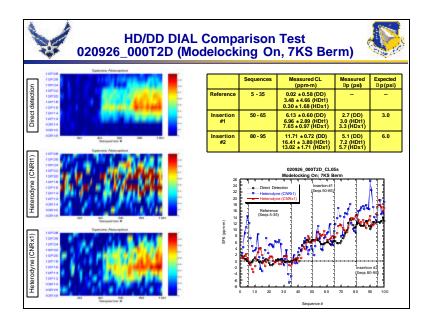


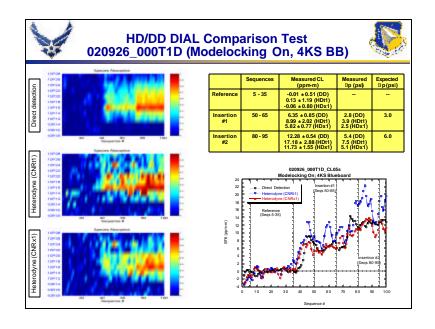


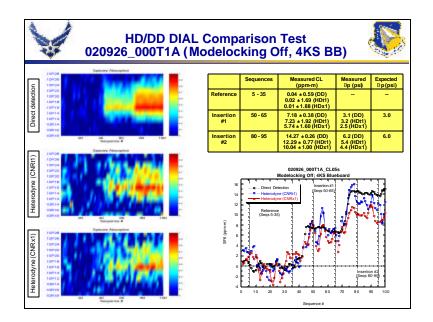


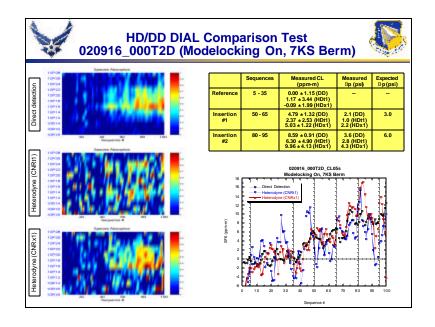


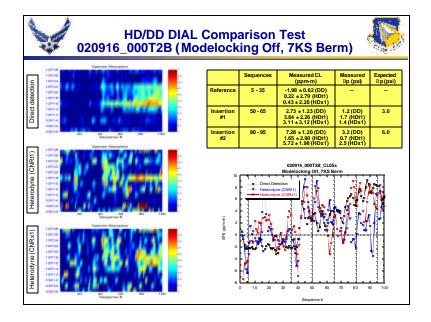


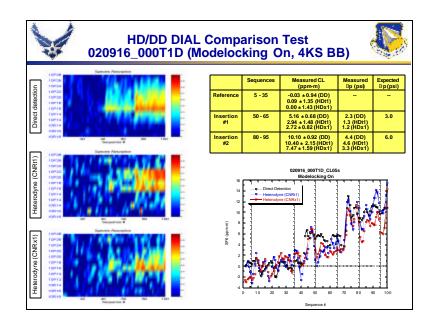


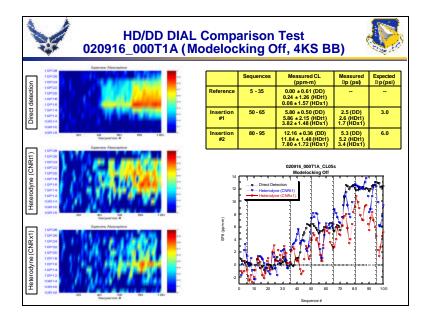


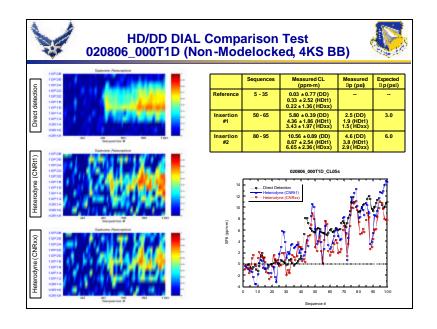


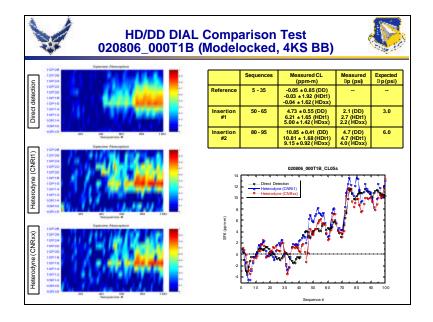


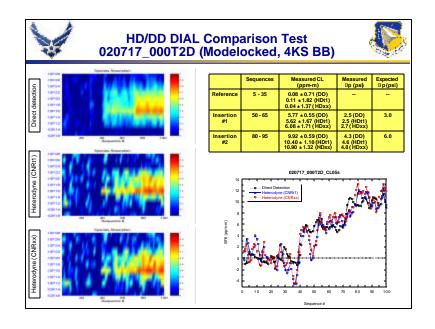


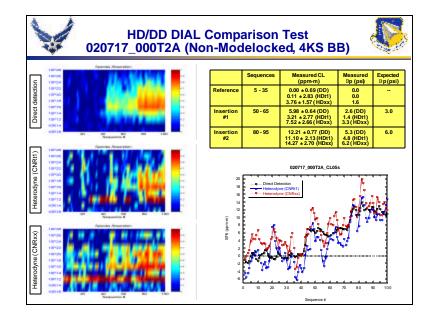


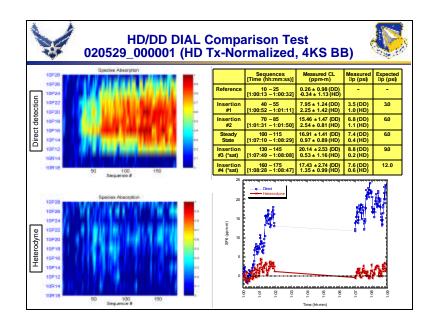


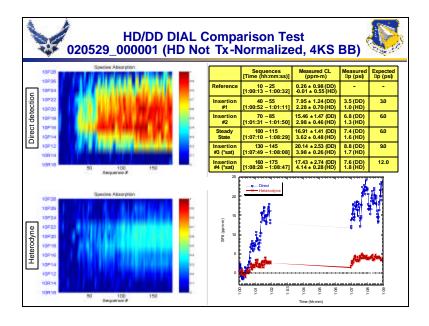


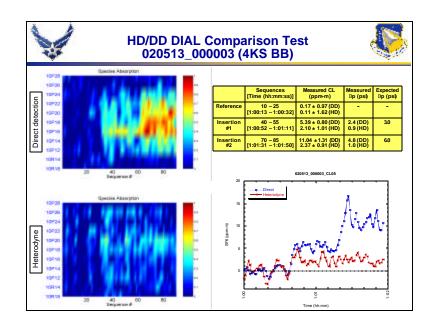


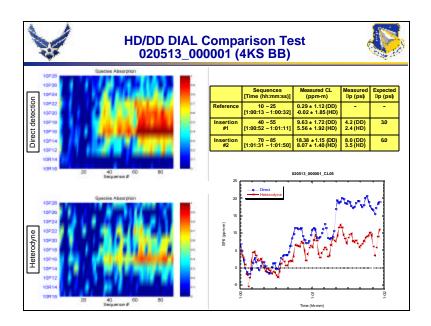












## Appendix C. MATLAB Programs

## **Appendix C Contents**

Section C1 - DATREDUC.m - Direct Detection Data Reduction

Section C2 - DATREDUC\_HD\_X3.m - Heterodyne Detection Data Reduction Section C3 - HDPulseSim.m - Heterodyne Pulse Simulation (Optical Field Based)

## C1. DATREDUC.m - Direct Detection Data Reduction

```
8/26/04 2:36 PM C:\ROS\DataAnalysis\ROSProgs\Reduction\DATREDUC.m
% Matlab program DATREDUC.M
   Created from ENERGY.M 30 Sep 96 by D.C. Senft
 \ Computes reduced data parameters from N-ABLE digitized waveform data
      (U, Vpk, tpk, dteff, Vrms, Vref)
    Modifications -
    24 Oct 96 - Transferred from Senft PMac to GLAPS
09 Jan 97 - Plotted signal and reference windows on overlay plot, rather
                   than on average plot
    07 May 97 - Corrected Vpk calculation to be referenced from Vref baseline,
                   rather than 0 V
    07 Jun 97 - Corrected tpk calculation to be referenced from start of
                   data window, rather than start of signal window
    Arrays work in Matlab-preferred column format, not row format

    n is pulse # (varies horizontally)
    i is sample # (varies vertically)

      . data(i-row,n-column)
    1 tau intra-pulse (sampling) time
    t pulse time

1 lambda wavelength, laser line
n Npulse pulse number
    m Nseq sequence number
   --- Processing ---
%fprintf(' \n')
%fprintf(' Nseq - %d\n', Nseq)
%fprintf('Nlines = %d\n',Nlines)
%fprintf('Npulses = %d\n',Npulses)
%fprintf(' Nsamples = %d\n', Nsamples)
t = tsample
tmin = min(t)
tmax - max(t)
for n=1:Npulses
  Np (n) =n
end
for m=1:Nseq
  Nn (m) =n.
end.
% <<< Convert from digitizer units to voltage >>>
```

```
8/26/04 2:36 FM C:\ROS\DataAnalysis\ROSProgs\Reduction\DATREDUC.m
           (' \n')
('Digitizer units to voltage conversion \n')
fprintf
fprintf
                  (' N-ABLE (*(1/4096)-0.100) [N] \n')
(' LARS (*(2/4096)-1.000) [L] \n')
fprintf
fprintf (' LARS (*(2/4096)-1.000) [L] \n')
fprintf (' HE-DAS (+1) [H] \n')
fprintf (' Kolmar (+1) [K] \n')
data2volt = input(' Brimrose (-1) [B): ', 's')
if ((data2volt=-'N'))(data2volt=-'n'))
data=data.*(1/4096)-0.100
elseif ((data2volt--'L'))(data2volt--'l'))
                                                                            .
 data=data.*(2/4096)-1.000
elseif ((data2volt=='H'))(data2volt=='h'))
 data-data
elseif ((data2volt=='K')|(data2volt=='k'))
  data=data
elseif ((data2volt=='B')|(data2volt=='b'))
 data=-data
end.
% -----<- Average pulses for each laser wavelength >>>-----
avgdata = zeros(Nsamples, Nlines)
for 1=1:Nlines
  for m=1:Nseq
   n=(m-1)*Nlines+1
   avgdata(:,1)=avgdata(:,1)+data(:,n)
  end
  avgdata(:,1)=avgdata(:,1)/Nseq
end
% ----<<< Plot overlayed pulses >>>-----
Nrows = 4
Nfrows= Nrows
Ncols = fix((Nlines-1)/Nrows)+1
Nfcols = Ncols
if (Nlines==1)
  Nfrows=2
  Nfcols=2
end
if (Ncols<2)
 Nfcols=2
%%%figure('Position',[10,40,300*Nfcols,225*Nfrows])
NlinesCh = Nlines
for 1ch-1:NlinesCh
```

```
8/26/04 2:36 PM C:\ROS\DataAnalysis\ROSProgs\Reduction\DATREDUC.m
end
                                                                                      ,
1f(Nlines>20)
 clear Chline
  while (1)
disp(' ')
disp(' *** Choose lines to be diplayed ***')
disp(' *** <ret> to continue ***')
t disp(' ')
    LineUsage=zeros(1,99)
LineUsage=LineUsage-1
    LineIndex0 = rem(LineIndex, 100)
    for 1-1:Nlines
     LineUsage(LineIndexO(1,1))=0
    end
    LineChoice
    pause
    NlinesCh = 0
    for 1=1:Nlines
     if(LineUsage(LineIndexO(1,1))==1)
NlinesCh = NlinesCh + 1
        ChLine (NlinesCh) =1
     end
    end
    1f(NlinesCh==0)
      disp(' ')
disp(' *** No lines chosen for display ***')
disp(' *** <ret> to continue ***')
disp(' ')
       pause
    elseif (NlinesCh>20)
     disp(' '" Maximum of 20 lines may be chosen """)
      disp(' ')
      pause
    else
      break
     end
end
```

```
8/26/04 2:36 FM C:\ROS\DataAnalysis\ROSProgs\Reduction\DATREDUC.m
 for 1ch-1:NlinesCh
   figure('Position',[30+40*(lch-1),500-40*(lch-1),500,400])
end
sigref-'N'
if (batchflg==0)
 TilePlot
end
surfdispflg = 'N'
                                                                   ; % Surface plot?
disp(' ')
surfquery=input('Surface plot (Y/[N]): ','s')
if ((surfquery=-'Y'))(surfquery=-'y'))
  SURFDISP_B
  while (1)
   fprintf(' \n')
               'New surface plot
'Print (B&M)
'Print (color)
    fprintf(
                                         [S] \n')
    fprintf(
                                        (P/BW) \n')
    fprintf(
                                         (C1')
                                         ( 1): ','8')
    query-input('Continue
    1f((query=='S')|(query=='s'))
      SURFDISP B
    elseif((query=='P')|(query=='p'))
      print
    elseif((query=='EN')|(query=='bw'))
    elseif((query=='C'))(query=='C'))
print -dpsc -Pcolor
    else
     break
    end
  end
end
if (batchflg==0)
 if(surfdispflg=='Y')
   delete(Nlines+1)
 end
end
%%%OverlayPlot
SigRefQuery
for 1ch=1:NlinesCh
 figure (1ch)
  PlotSigRef
end
Query
while (sigref=-'Y')
                                                                   # % Plot loop
```

```
8/26/04 2:36 PM C:\ROS\DataAnalysis\ROSProgs\Reduction\DATREDUC.m
TilePlot
PlotSigRef
   Query
 end
if(batchflg==0)
 for 1ch=1:NlinesCh
    delete(1ch)
  end
 end
clear NlinesCh ChLine
if (batchflg==0)
  figure('Position',[10,40,567,405])
% ----- <<< Begin integrated signal calculations >>>-----
Nt_s1 = t_s1/delt
Nt_s2 = t_s2/delt
Nt_r1 = t_r1/delt
Nt_r2 = t_r2/delt
if Nt_s1 <= 0
 Nt_s1=1
end
if Nt_s2 > Nsamples
  Nt_s2 = Nsamples
end
if Nt_r1 <= 0
 Nt_r1=1
end
if Nt_r2 > Nsamples
 Nt_r2 = Nsamples
Nt_s = Nt_s2-Nt_s1+1
Nt_r = Nt_r2-Nt_r1+1
Usig = zeros(Nseq, Nlines)
 Uref = zeros(Nseq, Nlines)
Vref = zeros(Nseq, Nlines)
U = zeros(Nseq,Nlines)
```

```
8/26/04 2:36 PM C:\ROS\DataAnalysis\ROSProgs\Reduction\DATREDUC.m
```

```
fprintf('\n')
for 1=1:Nlines
  fprintf(' Reducing laser line %d of %d (Step 1/3) \r',1,Nlines) ;
  for m=1:Nseq
    n=(n-1)*Nlines+1
    meandat-sum(data(Nt_r1:Nt_r2,n))/Nt_r
    Uvar=0.0
    for i=Nt_r1:Nt_r2
     Uref(m, 1) -Uref(m, 1) +data(i, n) *delt
     Uvar=Uvar+(data(i,n)-meandat)*(data(i,n)-meandat)*delt
    end
   Vref(n,1)=Uref(n,1)/(Nt_r*delt)
Vrms(n,1)=sqrt(Uvar/(Nt_r*delt))
  end
end
% fprintf('\n')
for 1=1:Nlines
 fprintf(' Reducing laser line %d of %d (Step 2/3) \r',1,Nlines) ;
  for m=1:Nseq
   n=(m-1)*Nlines+1
    (Vpk(n,1),pkindex)=max(data(Nt_s1:Nt_s2,n))
    Vpk(m,1)=Vpk(m,1)-Vref(m,1)
   tpk(m,1)=tsample(pkindex)
    tpk(m,1)=tsample(pkindex+Nt_s1-1)
    for i-Nt_s1:Nt_s2
     Usig(m,1)=Usig(m,1)+data(i,n)*delt
    end
 end
end
% fprintf('\n')
for 1=1:Nlines
 fprintf(' Reducing laser line %d of %d (Step 3/3) \r',1,Nlines) ;
  for m=1:Nseq
   n=(m-1)*Nlines+1
    U(m,1)=Usig(m,1)-(Nt_s*delt)*Vref(m,1)
   effwid(m,1)=U(m,1)/Vpk(m,1)
 end
end
fprintf('\n')
Uavg=sum(U)/Nseq
if (batchflg--0)
  first = 1
  while (1)
    if (first-1)
     plot (Nm, U*10^9)
      if(Nlines--1)
```

```
8/26/04 2:36 FM C:\ROS\DataAnalysis\ROSProgs\Reduction\DATREDUC.m
     title([TRtype, ' File = ',file])
      end
     xlabel('Pulse Number')
     ylabel('U (nV.s)')
      av=axis ; xmn=av(1) ; xmx=av(2) ; ymn=av(3) ; ymx=av(4)
     if (TRtype=='Tx')
      axis([xmn xmx min(0,ymn) ymx])
     end
     first = 0
    end
    replot=input('Rescale plot (Y/P/[N]): ','s')
    if((replot=='P')|(replot=='p'))
     print
   elseif((replot=='BW'))(replot=='bw'))
     print
   elseif((replot=='C')|(replot=='c'))
     print -dpsc -Pcolor
   elseif((replot-='Y')&(replot-='y'))
     break
     xmin=input('Enter new X min: ')
     xmax=input('Enter new X max: ')
     ymin=input('Enter new Y min: ')
     ymax-input('Enter new Y max: ')
     axis([xmin xmax ymin ymax])
   end
 end
end
%Eplot = input('Convert to energy (Y/[N]): ','s')
%if((Eplot=='Y')|(Eplot=='y'))
Ne-input('Enter conversion factor (V/W or V.s/J); ')
% first = 1
% while (1)
    if (first)
     plot (Nm, U/Rv)
      title([TRtype,' File = ',file,' Average = ',num2str(Uavg/Rv), ...
        . (3)
                  ','SDev = ',num2str(100*Usdev/Uavg),' [%]'])
      xlabel('Pulse Number')
      ylabel('Energy (J)')
      first = 0
     end
    replot=input('Rescale plot (Y/[N]): ','s')
     if((replot--'Y')&(replot--'y')) break; end
     xmin=input('Enter new X min: ')
     xmax=input('Enter new X max: ')
    ymin-input('Enter new Y min: ')
    ymax=input('Enter new Y max: ')
     axis((xmin xmax ymin ymax))
```

```
8/26/04 2:36 PM C:\ROS\DataAnalysis\ROSProgs\Reduction\DATREDUC.m
hend
%rect = [500,40,567,405]
%LARSHist-figure('Position', rect)
Whist (U/Davg, 100)
htitle({TRtype,' File = ',file,' U Histogram (',num2str(Npulses), ...
t ' pulses total) '])
%xlabel('Normalized Signal')
%ylabel('Number of Occurrences')
twhile(1)
% ascout=input('Write ASCII file for histogram (Y/[N]):','s') ;
% if((ascout~='Y')&(ascout~='y')) break; end ;
% [frequ uuu]=hist(U/Uavg,100) ;
% frequ=frequ/Npulses
% save uuu.asc uuu -ascii -double
% fprintf(' \n')
% fprintf(' Files frequ.asc and uuu.asc written ')
break; end
if(batchflg==0)
 delete(1)
% delete(2)
end
```

## C2. DATREDUC\_HD\_X3..m - Heterodyne Detection Data Reduction

```
8/26/04 3:17 PM C:\ROS\DataAnalysis\ROSProgs\HD-DD DC\DATREDUC_HD_X3_vRep.m
* DATREDUC HD X3
 W Created by DCS from DiegoProcessing DCS, originally written by
 N Diego Pierrottet, Dan Eckelkamp-Baker, and Dan Senft
 14 Nov 02 - Changed computation of CNRx1 to use Welch periodograms with equal signal
                 and noise windows in order to match resolutions for normalization
                 (division). Renamed CNRx3.
% Demultiplexing the raw data into its respective wavelength.
% No header file is used for this version.
% Wavelength sequence assumed to be standard 13 wavelengths,
% starting with 10R18,10P10,10P12,...,10P30
NDS close all
NDS clear all
NDS pack
Tstart = cputime
disp(' ')
disp(' ')

sa = input(' Enter sampling frequency (Hz) [le9] : ');

delt = 1/se

FRF = input(' Enter FRF (Hz) [10] : ');

Nseq = input(' Enter Nseq [101] : ');

Nlines = input(' Enter Nlines [13] : ');

disp(' ')
SigRefQueryl
                                                                  : % t_s1,t_s2,t_r1,t_r2 (sec)
Nt_s1 = round(t_s1/delt)+1
Nt_s2 = round(t_s2/delt)
Nt_r1 = round(t_r1/delt)+1
Nt_r2 = round(t_r2/delt)
TestFig = 0
                                                          ; % Normal (0) or test (1) read-in
if (TestFlg--0)
                                                         ; % Normal read-in
  disp(' ')
  disp(' Reading in TestHDDD.txt ')
disp(' ')
  load TestHDDD.txt
   NDS pickfile
   MDS load (together)
   TotalPoints-length (TestHDDD)
```

```
8/26/04 3:17 PM C:\ROS\DataAnalysis\ROSProgs\HD-DD_DC\DATREDUC_HD_X3_vRep.m
  PointsPerShot=TotalPoints/Nseq/Nlines
  %PointsPerShot=20004
  %Form data array: data(point, shot, line)
  data-zeros (PointsPerShot, Nseq, Nlines)
  for mm = 1:Nseq
    for 11 = 1:Nlines
      Npt1=round(((mn-1)*Nlines+ll-1)*PointsPerShot+1)
Npt2=round(((mn-1)*Nlines+ll)*PointsPerShot)
      data(:,mm, 11) = TestHDDD(Npt1:Npt2,1)
    if(Npt1~=round(Npt1));BBflg=1;keyboard;end
if(Npt2-=round(Npt2));BBflg=2;keyboard;end
   end
  end
  Nseq=Nseq-1
  data-zeros(PointsPerShot, Nseq, Nlines) ; % 030828_T2A manual correction
  for mm = 1:Nseq
   for 11 = 1:Nlines
     nn=(mm-1)*Nlines+11
      Nptl=round((nn-1)*PointsPerShot*i)
Npt2=round(nn*PointsPerShot*i)
                                                     /% skip bad pulse (#1056)
      Npt2=round(nn*FointsPerShot)
      data(:,nm,11)=TestHDDD(Npt1:Npt2,1)
   end
  end
  end
  clear TestHDDD
  pack
                                                     ; % Test read-in
else
 load TestMHDDD
 data - xdata
                                                      ;
  clear xdata
 Nseq = 10
time=1/sa:1/sa:PointsPerShot/sa
disp(' ')
```

```
8/26/04 3:17 PM C:\ROS\DataAnalysis\ROSProgs\HD-DD DC\DATREDUC HD X3 vRep.m
disp(' Starting Noise PSD calculation loop')
disp(' ')
Npts = max(Nt_s2-Nt_s1+1,Nt_r2-Nt_r1+1)
NFFTbase = ceil(log2(Npts))
NFFT = 2^NFFTbase
for nm = 1:1:Nseq
 for 11 = 1:1:Nlines
    noise=data(Nt_r1:Nt_r2,mm,11)
% [Pnn,fn]=pwelch(noise,[],[],NFFT,sa)
                                                            ; % use pdgrm for more accur spur calc
    [Pnn,fn]=periodogram(noise,[],NFFT,sa)
   NoisePSD(:,mm,ll)=Pnn
  end
end
disp(' Done Noise PSD calculation loop')
disp(' ')
N Rearrange data into correct wavelength sequence order
disp(' Starting spur frequency loop')
disp(' ')
del_fn = fn(2)
                                                                      ; % find spur frequencies
N_fnl = round((75.0e6-fn(1))/del_fn)
N_fn2 = round((81.0e6-fn(1))/del_fn)
for mm = 1:Nseq
  for 11 = 1:Nlines
    [YY, Nindex(mm, 11)] = max(NoisePSD(N_fn1:N_fn2,mm, 11))
    \begin{aligned} & \text{SpurFreq}(\text{nn,11}) = \text{fn}(\text{Nindex}(\text{nn,11}) + \text{N_fn1+1}) \\ & \text{SF\_Index}(\text{nn,11}) = \text{nm} + (11-1)/\text{Nlines} \end{aligned} 
  end
end
qqspur = median(SpurFreq)
figure('Position',[ 50 400 400 300])
plot(SF_Index,SpurFreq/le6, '.-')
title('Spur Frequencies (MHz)')
av=axis ; xmn=av(1) ; xmx=av(2) ; ymn=av(3) ; ymx=av(4)
axis([0 Nseq+1 ywn ymx])
figure('Position',[500 400 400 300])
plot(qqspur/le6)
hold on
plot(qqspur/le6, 'bx')
title('Median Spur Frequency (MHz)')
disp(' Arranging data into correct wavelength order')
```

```
8/26/04 3:17 FM C:\ROS\DataAnalysis\ROSProgs\HD-DD DC\DATREDUC_HD_X3_vRep.m
                                                                                    4 of 11
1 Rearrangement assumes first wavelength in sequence is always lowest wavelength, and
% therefore highest spur frequency
4 Throw out pulses prior to first occurrence of maximum spur frequency, will cause loss
% of one sequence
[YY, maxIndex] = max(qqspur)
                                                    1
for mm1=1:Nseq-1
 for ww1=1:Nlines
   nn0=(mm1-1)*Nlines+wwl+maxIndex-1
    mm0=floor((nn0-0.5)/Nlines)+1
    ww0=nn0-(nn0-1)*Nlines
   data(:,mm1,ww1)=data(:,mm0,ww0)
  end
end
data(:,Nseq,:) = 0
                                                   ; % Clear remainder of orig last seq
Nseq = Nseq-1
query=input(' Enter <ret> to continue : ','s');
clear NoisePSD
pack
& Calculate PSDs
disp(' ')
disp(' Starting PSD calculation loops')
disp(' ')
                                                              1
Nt_s = Nt_s2-Nt_s1+1
Nt_r = Nt_r2-Nt_r1+1
if(Nt_s<Nt_r)
disp(' ** Nt_s < Nt_r ** ')</pre>
 keyboard
end
Npts = Nt_r
NFFTbase = ceil(log2(Npts)+1)
NFFT = 2^NFFTbase
NLen = NFFT
                                                             ;% for periodograms
NLen = NFFT/4
                                                             ; % for Welch periodograms
NoisePSD = zeros(NLen/2+1, Nseq, Nlines)
SignalPSD = zeros(NLen/2+1, Nseq, Nlines)
```

scl = 1

```
8/26/04 3:17 PM C:\ROS\DataAnalysis\ROSProgs\HD-DD DC\DATREDUC HD X3 vRep.m
if(Nlines>=30)
 Y0 = 700
  sc1=1/2
  sc2=2/3
end
tmn = time(1)
tmx = ceil(time)
for mn=1:Nseq
 fprintf(' Sequence #: %d \n',mm)
  for 11=1:Nlines
  figure('Fosition',[25+25*(11-1)*sc1,Y0-20*(11-1)*sc1,800*sc2,700*sc2])
% figure('Position',[25+25*(11-1)*sc1,Y0-25*(11-1)*sc1,800*sc2,300*sc2], ...
         'Name', LineName (LineIndex(1,11),:))
% text(xmx-0.15*(xmx-xmn),ymx-0.05*(ymx-ymn), ...
% LineName(LineIndex(1,11),:), 'Color', [0 1 1])
                                                       # % Time series
  subplot (4,1,1)
  plot(time*le6,data(:,mm,ll))
  set(gca, 'FontBize', [9])
% set(gca,'YTickLabel',[])
  title('Time Series')
  av=axis / xmn=av(1) / xmx=av(2) / ymn=av(3) / ymx=av(4) /
  axis([0 20 -1.0 1.0])
  hold on
  PlotSigRef1
                                                        ; % display sig and ref windows
  subplot (4,1,2)
                                                           ; % Signal (Rx) and noise PSDs
  plot(fn/le6, NoisePSD(:,mm, 11), 'r-')
  hold on
  plot(fn/le6,SignalPSD(:,mm,11), 'g-')
% plot(fn,NormPSD(:,mm,ll),'b-')
  set(gca, 'FontBize', [9])
% set(gca,'YTickLabel',[])
  title('Rx and Nz PBDs')
  av=axis ; xmn=av(1) ; xmx=av(2) ; ymn=av(3) ; ymx=av(4)
  axis([0 200 min(0,ymn) ymx])
  hold on
  subplot (4,1,3)
                                                          ; 4 Signal PSD
  plot(fn/le6,SignalPSD(:,mm,ll)-NoisePSD(:,mm,ll))
% plot(fn,NormPSD(:,nm,ll),'b-')
  set (gca, 'FontSize', [9])
% set(gca,'YTickLabel',[])
  title('Signal PSD')
  av=axis ; xmn=av(1) ; xmx=av(2) ; ymn=av(3) ; ymx=av(4)
  axis([0 200 min(0,ymn) ymx])
  hold on
```

```
8/26/04 3:17 FM C:\ROS\DataAnalysis\ROSProgs\HD-DD DC\DATREDUC HD X3 vRep.m
  subplot (4,1,4)
  plot(fn/le6,NormPSD(:,mm,ll))
  set(gca, 'FontSize',[9])
% set(gca,'YTickLabel',[])
  title('Normalized PSD')
  av=axis ; xmn=av(1) ; xmx=av(2) ; ymn=av(3) ; ymx=av(4)
  axis([0 200 min(0,ymn) ymx])
  hold on
  end
 fprintf (' Enter <ret> to continue \n')
query*input(' Enter <s> to stop displays
                                                   : ','=') ;
  delete(1:Nlines)
  if((query=-'S'))(query=-'s')); break; end
end
disp(' ')
                                                               1
disp(' Starting CNR calculation loops')
disp(' ')
                                                              .
% *** CNRt1 ***
RR = zeros(Nseq,Nlines)
NN = zeros(Nseq,Nlines)
CNRt1 = zeros(Nseq, Nlines)
% Compute DC for p(t) in signal and noise windows
for mm=1:Nseq
 for 11-1:Nlines
   DCsig(mm,11) = mean(data(Nt_s1:Nt_s2,mm,11))
   DCnz(mm, 11) = mean(data(Nt_r1:Nt_r2,mm, 11))
  end
end
% Compute return power, noise power, (signal power), and CNRt1
for mm=1:Nseq
 for 11=1:Nlines
   RRt1(mm, 11) = ...
     sum ((data(Nt_s1:Nt_s2,mm,11)-DCsig(mm,11)).*(data(Nt_s1:Nt_s2,mm,11)-DCsig(mm,11)));
     sum((data(Nt_r1:Nt_r2,mm,11) - DCnz(mm,11)).*(data(Nt_r1:Nt_r2,mm,11) - DCnz(mm,11)));
   CNRt1(mm, 11) = (RRt1(mm, 11)/(((Nt_s2-Nt_s1+1)/(Nt_r2-Nt_r1+1))*NNt1(mm, 11)))-1
  end
end
```

```
8/26/04 3:17 FM C:\ROS\DataAnalysis\ROSProgs\HD-DD DC\DATREDUC HD X3 vRep.m
* *** CNRf1 ***
for mm=1:Nseq
 for 11-1:Nlines
   RRf1(nm,11) = sum(SignalPSD(:,nm,11))
NNf1(nm,11) = sum( NoisePSD(:,nm,11))
CNRf1(nm,11) = RRf1(nm,11)/NNf1(nm,11)-1
  end
end.
*** CNRx3 - Point-by-point frequency normalization ***
% ExcessNzFactor = 0.1785
% ExcessNzFactor = 0.750
                                                    ;% approx CNRx1 random noise div factor
                                                   7% approx CNRx2 random noise div factor
ExcessNzFactor = 0.150
                                                   ; % approx CNRx3 random noise div factor
SNR = sum (NormPSD-1-ExcessNzFactor)
for mm = 1:Nseq
 for 11 = 1:Nlines
   CNRx3(mm, 11) = (1/(NFFT/2+1))*SNR(1, mm, 11) ; % scale factor is only approximate
end
% *** Display CNRs ***
% Smooth CNRs to reduce effects of single point nonlinearies in scale factors
Tsmooth = 10
                                                   ; % set smoothing extent (sec)
for mm=1:Nseq
                                                   ; % create pulse time for Hanning_TSmooth
 for 11-1:Nlines
   nn=(mm-1)*Nlines+11
   tpulse(mm, 11) = (nn/PRF)/3600
                                                   ; % approximate pulse time (hh.ddd)
  end
end
Hdata = CNRt1
Henning_TSmooth
qq_t1 = Hdata
Hdata - CNRf1
Hanning_TSmooth
qq_f1 - Hdata
Hdata = CNRx3
Hanning_TSmooth
qq_0 = Hdata
```

```
8/26/04 3:17 PM C:\ROS\DataAnalysis\ROSProgs\HD-DD_DC\DATREDUC HD_X3 vRep.m
Scl_flt1 = mean(qq_fl./qq_tl)
sc1_0t1 = mean(qq_0./qq_t1)
for 11=1:Nlines
  figure('Position',[25+25*(11-1)*sc1,Y0-20*(11-1)*sc1,600*sc2,700*sc2])
                                                               ; % Scaled CNRs overlay
  subplot (4, 1, 1)
  plot(CNRt1(:,11), 'k-')
  hold on
 plot(CNRf1(:,11)./scl_f1t1(1,11), 'g-')
plot(CNRx3(:,11)./scl_0t1(1,11), 'r-')
set(gca, 'FontSize', [9])

set(gca, 'YTickLabel', [])
 title('Overlayed Scaled CNRs')
  av=axis ; xmn=av(1) ; xmx=av(2) ; ymn=av(3) ; ymx=av(4)
  axis([xmn xmx min(0,ymn) ymx])
% hold on
 subplot (4, 1, 2)
                                                               : % CNRtl
 plot(CNRt1(:,11))
  set (gca, 'FontSize', [9])
% set(gca,'YTickLabel',[])
 title('CNRt1')
  av-axis ; xmn-av(1) ; xmx-av(2) ; ymn-av(3) ; ymx-av(4)
  axis([xmn xmx min(0,ymn) ymx])
hold on
                                                              ) % CNRfl
 subplot (4,1,3)
  plot(CNRfl(:, ll))
set(gca, 'FontSize',[9])
set(gca, 'YTickLabel',[])
 title('CNRf1')
  av=axis ; xmn=av(1) ; xmx=av(2) ; ymn=av(3) ; ymx=av(4)
  axis([xmn xmx min(0,ymn) ymx])
hold on
 subplot (4,1,4)
                                                               7 % CNRx3
 plot(CNRx3(:,11))
 set(qca, 'FontSize', [9])
% set(gca, 'YTickLabel', [])
 title('CNRx3')
 av-axis ; xnn-av(1) ; xnx-av(2) ; ynn-av(3) ; ynx-av(4)
  axis([xmn xmx min(0,ymn) ymx])
% hold on
```

```
8/26/04 3:17 PM C:\ROS\DataAnalysis\ROSProgs\HD-DD_DC\DATREDUC_HD_X3 vRep.m
disp(' Done CNR calculation loop');
disp(' ');
*** Save CNRs ***
save HDDD CNRt1 CNRf1 CNRx3
disp(' HDDD.mat saved');
disp(' ');
Tend = cputime-Tstart
% Tend
delete(1)
Plots for selected sequences
while (query-=0)
  mm = query
  Y0 - 400
  sc1 = 1
sc2 = 1
  if(Nlines>=30)
   Y0 = 700
   sc1=1/2
   sc2=2/3
  end
  tmn = time(I)
  tmx = ceil(time)
% fprintf(' Sequence #: %d \n',mm)
 for 11=1:Nlines
 figure('Position',[25+25*(11-1)*scl,Y0-20*(11-1)*scl,800*sc2,700*sc2])
% figure('Position',[25+25*(11-1)*sc1,Y0-25*(11-1)*sc1,800*sc2,300*sc2], ...
        'Name', LineName (LineIndex(1,11),:))
% text(xmx-0.15*(xmx-xmn),ymx-0.05*(ymx-ymn), ...
% LineName(LineIndex(1,11),:),'Color',[0 1 1])
  subplot (4,1,1)
                                                     ; % Time series
  plot(time*le6,data(:,mm,ll))
  set(gca, 'FontSize',[9])
```

```
8/26/04 3:17 FM C:\ROS\DataAnalysis\ROSProgs\HD-DD DC\DATREDUC HD X3 vRep.m
% set(gca, 'YTickLabel',[])
 title('Time Series')
  av=axis ; xmn=av(1) ; xmx=av(2) ; ymn=av(3) ; ymx=av(4) ;
  axis([0 20 -1.0 1.0])
% axis([0 100 -1.0 1.0])
  hold on
                                                            ; % display sig and ref windows
  PlotSigRefl
  subplot (4,1,2)
                                                                  : % Sig (rcv) and noise PSDs
  plot(fn/1e6, SignalFSD(:, mm, ll), 'g-')
  hold on
  plot(fn/le6, NoisePSD(:, mm, 11), 'r-')
plot(fn,NormPSD(:,mm,ll),'b-')
set(gca,'FontSize',[9])
* set(gca,'YTickLabel',[])
 title('Rx and Nz PSDs')
  av-axis ; xmn-av(1) ; xmx-av(2) ; ymn-av(3) ; ymx-av(4)
% axis([0 200e6 min(0,ymm) ymx])
  axia([0 500 min(0,ymn) ymx])
 hold on
 subplot (4,1,3)
                                                                ; % Signal PSD
  plot(fn/le6,SignalPSD(:,mm,ll)-NoisePSD(:,mm,ll))
% plot(fn,NormPSD(:,mm,11),'b-')
set(gca,'FontSize',[9])
% set(gca,'YTickLabel',[])
  title('Signal PSD')
  av=axis ; xmn=av(1) ; xmx=av(2) ; ymn=av(3) ; ymx=av(4) ;
% axis([0 200e6 min(0,ymm) ymx])
  axis([0 500 min(0,ymn) ymx])
  hold on
 subplot(4,1,4)
                                                                ; % Normalized PSD
  plot(fn/le6,NormPSD(:,mm,11))
set(gca, 'FontSize', [9])

set(gca, 'YTickLabel', [])
 title ('Normalized PSD')
  av=axis ; xnn=av(1) ; xnx=av(2) ; ynn=av(3) ; ynx=av(4)
% axis([0 200e6 min(0,ymm) ymx])
  axis([0 500 min(0,ymn) ymx])
  hold on
  disp(' ')
fprintf (' Enter seq # to display \n')
query=input(' Enter <0> to stop : ')
  delete(1:Nlines)
```

## C3. HDPulseSim..m - Heterodyne Pulse Simulation (Optical Field Based)

```
8/26/04 3:38 FM C:\LROS\Models\Heterodyne Pulse Simulation\HD...\HDPulseSim.m
Matlab program HDPulseSim.m
    Program to simulate modelocked laser pulse in both temporal and frequency space
   Created 14 Mar 03 by D.C. Senft
    Modifications
      dd mmm yy - xxx
pack
warning off
                                                       ; \ use only on 5.x
% UserID = 'LAPS '
% UserID = 'GLAPS '
% UserID = '7658CIF_PC'
| UserID = 'Senft_NTPC'
| UserID = 'Senft_LT' '
xxx = computer
platform = xxx(1:4)
clear xxx
                                     ; % initialize random # generator
; % initialize Gaussian random # generator
rand('state', sum(100*clock))
randn('state', sum(100*clock))
% Constants (physical and system)
wvl = 10.591e-6 ; % wavelength (C12-O16 10F20)
Tsam = 1e-9 ; % DAC sampling interval
BM_DAC = 1/(2*Tsam) ; % data collection bandwidth
LL = 3.5 ; % cavity length (m)
delf_IF = 13.7e6 ; % freq offset between Rx and LO (Hz, actually random)
& Create modelocked temporal pulse
TT
        = 20e-6
                                                      ; & time window
      = 0.2*1e-9
= TT/dt
= 1e-9
                                                      ; & time point spacing
dt
Nt
                                                      ; & number of temporal points
                                                       ; % actual system sampling interval
```

```
8/26/04 3:38 FM C:\LROS\Models\Heterodyne Pulse Simulation\HD...\HDPulseSim.m
                                                    ; % actual number of sample points
      = zeros(1,Nt)
= zeros(1,Nt)
tt1
tt_Dt = zeros(1,N_Dt)
       = zeros(1,Nt)
= zeros(1,Nt)
= zeros(1,Nt)
= 1
99
G1
sig1 = 0.4e-6
                                          ; % width param of first Rician
        = 0.15
G2
G2 = 0.15

sig2 = 2.0e-6

siga = 1.30e-9

dt_a = 2*LL/cspeed

Nt_a = dt_a/dt+1
                                          ; % width param of second Rician
                                          ; % width of Gaussian temporal modes (~3 ns FWHM)
                                          ) % spacing between Gaussian temporal modes
                                           ; & number of points in single interval
for ii-1:N Dt
                                           ; % actual time samples
 tt_Dt(ii)=(ii-1)*Dt
end
for ii=1:Nt
 tt(ii)=(ii-1)*dt
                                ; % shift to start at 7 us to match real data
  tt1(ii)=tt(ii)-7e-6
  1f(tt(11)<=7e-6)
    gg(ii)=0.0
   gg(ii)=G1*(ttl(ii)/le-6)*exp((-ttl(ii)*ttl(ii))/(2*sig1*sig1)) + ...
G2*(ttl(ii)/le-6)*exp((-ttl(ii)*ttl(ii))/(2*sig2*sig2)) ;
      G2*(tt1(ii)/le-6)*exp((-tt1(ii)*tt1(ii))/(2*sig2*sig2))
  end
end
for li=1:Nt
                                           ; % create sequence of Gaussians
  tta=mod(tt(ii),dt_a)-dt_a/2
  aa(ii)=exp((-tta*tta)/(2*siga*siga)) ;
end
                                           ; % create ml pulse train with temporal envelope
pp = qg.*aa
                                           ; % pp is instantaneous power, square of field uu
figure('Position',[50 600 550 400])
plot(tt/le-6,gg)
hold on
plot(tt/le-6,aa,'r-')
plot(tt/1e-6,pp, 'g-')
ylabel ('Optical Power Components (Modelocked) (W)')
ylabel('Time (us)')
ylabel('Optical Fower (N)')
 av=axis ; xmn=av(1) ; xmx=av(2) ; ymn=av(3) ; ymx=av(4) ;
 axis([0 TT/le-6 ymm ymx])
hold off
```

```
8/26/04 3:38 PM C:\LROS\Models\Heterodyne Pulse Simulation\HD...\HDPulseSim.m
% Compute frequency spectrum for modelocked temporal pulse
NFFTbase = cell(log2(Nt))
NFFT - 2^NFFTbase
Fp = zeros(1,NFFT)

Fpp = zeros(1,NFFT)

freq = zeros(1,NFFT)

ppI = zeros(1,NFFT)

ttI = zeros(1,NFFT)
Fp = fft(pp*dt,NFFT)

Fpp = fftshift(Fp)

df = 1/(NFFT*dt)

BW = 1/(2*dt)
for jj-1:NFFT
 freq(jj)=(jj-NFFT/2-1)*df
end
figure('Position',[700 500 550 600])
subplot (3,1,1)
plot(freq/le6,abs(Fpp))
title('Optical Power Frequency Spectrum | Fpp|') ;
xlabel('Frequency (MHz)')
ylabel('Frequency Spectrum')
subplot (3,1,2)
plot(freq/le6, real(Fpp))
title('Optical Power Frequency Spectrum (Real(Fpp))') ;
xlabel('Frequency (MHz)')
ylabel('Frequency Spectrum')
subplot (3,1,3)
plot(freq/le6,imag(Fpp))
title('Optical Power Frequency Spectrum (Imag(Fpp))')
xlabel('Frequency (MHz)')
ylabel('Frequency Spectrum')
ppI = ifft(Fp*NFFT*df)
for 11=1:NFFT
 ttI(ii)=(ii-1)/(NFFT*df)
figure('Position', [50 50 550 400])
plot(ttI/le-6,ppI)
hold on
plot(tt/le-6,pp, 'g:')
title('Optical Power (IFFT) (W)')
xlabel('Time (us)')
ylabel('Optical Power (N)')
av-axis ; xmn-av(1) ; xmx-av(2) ; ymn-av(3) ; ymx-av(4) ;
axis([0 TT/le-6 ymm ymx])
```

```
8/26/04 3:38 FM C:\LROS\Models\Heterodyne Pulse Simulation\HD...\HDPulseSim.m
 Compute scale factor to normalize to received energy (integrated instantaneous power)
Epp = sum(pp)*dt
% Create quasi-cw LO waveform
pp_LO = zeros(size(pp))
pp_LOsc = zeros(size(pp))
Pp_LO = zeros(size(Fp))
Ppp_LO = zeros(size(Fp))
ppI_LO = zeros(size(ppI))
Pp_LOsc = zeros(size(Fp))
Pp_LOsc = zeros(size(Fp))
ppI_LOsc = zeros(size(Fp))
ppI_LOsc = zeros(size(ppI))
disp(' ')
a77 = input(' Enter 1st spur scale factor [0.8e-3]: ');
s154 = input(' Enter 2nd spur scale factor [1.2e-3]: ');
phi77 = 2*pi*rand
                                                           ; % arbitrarily chosen phase
phi77 = 2*pi*rand ; % arbitrarily chosen phase
phi154 = 2*pi*rand ; % arbitrarily chosen phase
% a nz = 1.0e-12 ; % noise level for LO spectrum
delf_LO = 77e6 ; % specing between LO main mode and spurs (H
% sigLO = 85e3 ; % spectral width of LO frequency modes (Hz)
                                                           ; % spacing between LO main mode and spurs (Hz)
for ii=1:Nt
 pp_LO(i1) = 1 + s77*cos(2*pi*delf_LO*tt(ii)+phi77) + ...
     s154*cos(2*pi*(2*delf_LO)*tt(ii)+phi154)
  pp_LOac(ii) = s77*cos(2*pi*delf_LO*tt(ii)+phi77) + ...
al54*cos(2*pi*(2*delf_LO)*tt(ii)*phil54) ;
end
Fp_LO = fft(pp_Lo*dt,NFFT)
Fpp_LO = fftshift(Fp_LO)
ppI_LO = ifft(Fp_Lo*NFFT*df)
Fp_LOac = fft(pp_LOac*dt,NFFT)
Fpp_LOac = fftshift(Fp_LOac)
ppI_LOac = ifft(Fp_LOac*NFFT*df)
figure('Position',[700 300 550 600])
 subplot (3,1,1)
plot(freq/le6,abs(Fpp_LO))
 hold on
plot(freq/le6,abs(Fpp_LOac), 'r-')
 title('LO Frequency Spectrum | Fpp_LO|')
xlabel('Frequency (MHz)')
 ylabel('Frequency Spectrum')
 subplot (3,1,2)
plot(freq/le6, real(Fpp_LO))
```

```
8/26/04 3:38 FM C:\LROS\Models\Heterodyne Pulse Simulation\HD...\HDPulseSim.m
plot(freq/le6, real(Fpp_LOac), 'r-')
title('LO Frequency Spectrum (Real(Fpp))')
xlabel('Frequency (MHz)')
ylabel ('Frequency Spectrum')
subplot (3,1,3)
plot(freq/le6,imag(Fpp_LO))
hold on
semilogy(freq/le6,imag(Fpp_LOac), 'r-')
title('LO Frequency Spectrum (Imag(Fpp))')
xlabel('Frequency (MHz)')
ylabel('Frequency Spectrum')
figure('Position',[700 50 550 400])
plot(ttI/le-6,ppI_LO)
hold on
plot(tt/le-6,pp_LO,'y:')
plot(ttI/le-6,ppI_LOac, 'r-')
plot(tt/le-6,pp_LOac, 'g:')
title('LO Optical Power (IFFT) (W)')
xlabel('Time (us)')
ylabel('LO Optical Power (W)')
av=axis ; xmn=av(1) ; xmx=av(2) ; ymn=av(3) ; ymx=av(4) ;
axis([0 TT/le-6 ymm ymx])
% Create Rx and LO optical field variables from optical power terms
uu_r = sqrt(pp)
uu_LO = sqrt(pp_LO)
Fu_r = fft(uu_r*dt,NFFT)
Fuu_r = fftshift(Fu_r)
Fu_LO = fft(uu_LO*dt,NFFT)
Fuu_LO = fftshift(Fu_LO)
& Display field / power temporal / spectral values
disp(' ')
disp(' ### Press return to continue ###')
disp(' ')
pause
disp(' Displaying field / power temporal / spectral values ') ;
disp(' ')
delete(1:5)
figure('Position',[ 50 600 550 400])
                                                  ; tF1 pp and uu_r temporal display
plot(tt/le-6,pp)
hold on
```

```
8/26/04 3:38 PM C:\LROS\Models\Heterodyne Pulse Simulation\HD...\HDPulseSim.m
plot(tt/le-6,uu_r, 'r:')
title('Optical Power (M)')
                                                ;
xlabel('Time (us)')
ylabel('Optical Power (W)')
figure('Position',[ 50 50 550 400]) / %FZ Fp and Fu_r spectral display (Fpp,Fuu_r)
subplot (2,1,1)
plot(freq/le6,abs(Fpp))
hold on
plot(freq/le6,abs(Fuu_r), 'r:')
title('Frequency Spectrum (Fower and Field, |Fp|, |Fu|')
xlabel('Frequency (MHz)')
ylabel('Frequency Spectrum')
subplot (2,1,2)
plot(freq/le6, angle(Fpp))
hold on
plot(freq/ie6, angle(Fuu_r), 'r:')
title('Frequency Spectrum Phase (Power and Field, Fp, Fu')
xlabel('Frequency (MHz)')
ylabel('Frequency Spectrum Phase')
figure('Position',[700 600 550 400])
                                               ; %F3 pp LO and uu LO temporal display
plot(tt/le-6,pp_LO)
hold on
plot(tt/1e-6,uu_LO, 'r:')
title('LO Optical Power and Field (W, sqrt(W))' ) ;
xlabel('Time (us)')
ylabel('Optical Power and Field')
figure('Position',[700 50 550 400]) ; %F4 Fp_LO and Fu_LO spectr disp (Fpp_LO,Fuu_LO)
subplot(2,1,1)
plot(freg/le6,abs(Fpp_LO))
hold on
plot(freq/le6,abs(Fuu_LO), 'r:')
title('LO Frequency Spectrum (Power and Field, [Fp_LO], [Fu_LO]') ; xlabel('Frequency (MHz)')
ylabel('Frequency Spectrum')
subplot (2,1,2)
plot(freq/le6,angle(Fpp_LO))
hold on
plot(freq/le6,angle(Fuu_LO), 'r:')
title('LO Frequency Spectrum Phase (Power and Field, Fp_LO, Fu_LO') xlabel('Frequency (MHz)')
ylabel('Frequency Spectrum')
1 Check that spectrum of received optical power is convolution of Rx opt field spectrum
icnvflg = 0
                                                        ; A execute flag
if (icnvflg==1)
  disp(' ### Rx convolution check routine ### ')
```

```
8/26/04 3:38 FM C:\LROS\Models\Heterodyne Pulse Simulation\HD...\HDPulseSim.m
  disp(' ### Press return to begin ###')
  disp(' ')
  pause
  disp(' Rx convolution check routine started')
  disp(' ')
  [aa Nsize] = size(Fuu_r)
  Nuse = 75000 ; % size of convolution xFu = Fuu_r(1; (Nsize/2-Nuse/2+1): (Nsize/2+Nuse/2)) ;
  xFp = Fpp(1, (Nsize/2-Nuse/2+1): (Nsize/2+Nuse/2))
  xFc = conv(xFu,xFu)*df
  xFc = xFc(1,Nuse/2+1:Nuse+Nuse/2)
                                                         : % overlay power and conv spectra
  figure('Position',[800 400 550 400])
  plot(abs(xFp))
  hold on
  plot(abs(xFc), 'r:')
end
% Check that spectrum of LO optical power is convolution of LO optical field spectrum
icnvflg = 0
                                                        # % execute flag
if (icnvflg--1)
 disp(' ### LD convolution check routine ### ')
disp(' ### Press return to begin ###')
  pause
  disp(' LO convolution check routine started')
  disp(' ')
  [aa Nsize] = size(Fuu LO)
  Nuse = 75000
                                                        ; % size of convolution
  xFu = Fuu_LO(1, (Nsize/2-Nuse/2+1): (Nsize/2+Nuse/2))
  xFp = Fpp_LO(1,(Nsize/2-Nuse/2+1):(Nsize/2+Nuse/2))
  xFc = conv(xFu, xFu)*df
  xFc = xFc(1,Nuse/2+1:Nuse+Nuse/2)
                                                         ; % overlay power and conv spectra
  figure('Position',[800 400 550 400])
  plot(abs(xFp))
  hold on
  plot(abs(xFc), 'r:')
end
Clear unneeded variables
clear as gg ppI ppI LO ppI LOac Fpp Ppp LO Fpp LOac uu r uu LO Fu r Fuu r Fu LO Fuu LO ;
% Calculate optical power signal on heterodyne detector
disp(' ### Calculation of optical power signal on heterodyne detector ### ' )
disp(' ### Press return to begin ###')
disp(' ')
pause
```

```
8/26/04 3:38 FM C:\LROS\Models\Heterodyne Pulse Simulation\HD...\HDPulseSim.m
disp(' Calculation started')
delete(1:4)
%--- Receive optical power scaling
Eppin - input(' Enter receive optical power on detector (pJ) [2.0]: ');
disp(' ')
Eppin = Eppin*le-12
                                                         ; % convert from pJ to J
                                                        1 % scale received optical power
pp = pp*(Eppin/Epp)
%--- LO optical power scaling
P_LOin = input(' Enter LO optical power on detector (nW) [0.125]: ') ;
disp(' ')
P_LOin = P_LOin*le-3
                                                        ; % convert from mH to W
                                                       ; A scale LO power
pp_LO = P_LOin*pp_LO
pp_LOac = P_LOin*pp_LOac
                                                        / % scale AC-coupled LO power
4--- Calculate LO shot noise optical power
%- Calculate for full temporal series, then scale and bandlimit to match DAC BW
sig_sn = sqrt({2*(hh*cspeed/wv1)*BW_DAC/qe_det)*mean(pp_LO)})
pp_sn = sig_sn*randn(size(pp_LO))
Fp_sn = fft(pp_sn*dt,NFFT)
Fpp_sn = fftshift(Fp_sn)
N_BWDAC = round(BW_DAC/df)
stp_fcn = zeros(1,NFFT)
stp_fcn(1,1:N_BWDAC) = 1
stp_fcm(1,NFFT-N_BWDAC+1:NFFT) = 1
                                                        .
Fp_sn = Fp_sn.*stp_fcn*sqrt(BW/BW_DAC)
Fpp_sn = fftshift(Fp_sn)
                                                       ; % scale to maintain noise power
ppI_sn = ifft(Fp_sn*MFFT*df,NFFT)
                                                        .
[AA BB] = size(pp_sn)
pp_sn = ppI_sn(1,1:BB)
                                                         ;
1--- Calculate heterodyne optical power on detector
%- Perform AC-coupling now to avoid errors from sinc distortion in numerical calc
pp_hd = pp + pp_LOac + 2*cos(2*pi*(delf_IF*tt)).*sqrt(pp.*pp_LO) + real(pp_sn) ;
Fp_hd = fft(pp_hd*dt,NFFT)
Fpp_hd = fftshift(Fp_hd)
```

```
8/26/04 3:38 PM C:\LROS\Models\Heterodyne Pulse Simulation\HD...\HDPulseSim.m
figure('Position',[100 700 550 400])
                                                  ; %Fig pp_hd temporal plot
plot(tt/le-6,pp_hd)
title('HD Optical Power (W)')
xlabel('Time (us)')
ylabel('Optical Power (W)')
% av=axis ; xmn=av(1) ; xmx=av(2) ; ymn=av(3) ; ymx=av(4) ;
% axis([xmn xmx 0 ymx])
                                                  / %Fig pp_hd spectrum
figure('Position',[100 100 550 500])
subplot(2,1,1)
plot(freq/le6,abs(Fpp_hd))
title('Frequency Spectrum (HD Optical Power)')
xlabel('Frequency (MHz)')
ylabel('Frequency Spectrum')
subplot (2,1,2)
plot(freq/le6,angle(Fpp_hd))
title('Frequency Spectrum Phase (HD Optical Power)' )
xlabel('Frequency (MHz)')
ylabel('Frequency Spectrum Phase')
% Calculate current (AC-coupled) out of detector (incl bias curr and b.c. shot noise)
I_hd = (qe_det*qq)/(hh*cspeed/wvl)*pp_hd
                                            ; % includes LO shot noise
%--- Compute bias current and bias current shot noise
disp(' ')
I_bias = input(' Enter bias current (mA) [0.100]: ') ;
I_bias = I_bias*le-3
disp(' ')
                                                  ; % convert from mA to A
sig_Ib = sqrt(2*qq*BW_DAC*I_bias)
                                                 ; % at dev of bias curr shot noise
i_bias = sig_Ib*randn(size(pp_hd))
                                                ; % bias current shot noise
Fi b = fft(i bias*dt,NFFT)
Fii_b = fftshift(Fi_b)
                                                   .
Fi_b = Fi_b.*stp_fcn*sqrt(BM/BW_DAC)
                                                  ; % scale to maintain noise power
Fii_b = fftshift(Fi_b)
iiz_b = ifft(Fi_b*NFFT*df,NFFT)
[AA BB] - size(i_bias)
i_bias = iiZ_b(1,1:BB)
i_bias = real(i_bias)
                                                   ; % force i_bias to be real
%--- Compute total AC-coupled current out of detector
```

```
8/26/04 3:38 FM C:\LROS\Models\Heterodyne Pulse Simulation\HD...\HDPulseSim.m 10 of 10
I_det = I_hd + i_bias
% Calculate voltage at input to A/D and reduce data to actual system sampling interval
Detector -> X74 amp -> 2 MHz high pass -> X22 amp -> 50-ohm A/D
V_AD0 - I_det * 74 * 1.0 * 22 * 50
V_AD = interpl(tt,V_ADO,tt_Dt)
NFFTDaseV = ceil(log2(N_Dt))

NFFTV = 2^NFFTbaseV

dfV = 1/(NFFTV^Dt)
for jj=1:NFFTV
 freqV(jj)=(jj-NFFTV/2-1)*dfV
FV AD = fft(V AD*Dt,NFFTV)
FVV_AD = fftshift(FV_AD)
figure('Position',[700 700 550 400]) ; %Fig V_AD temporal plot plot(tt Dt/ie-6,V AD) ;
title('Signal at A/D (V)')
xlabel('Time (us)')
ylabel('Signal at A/D (V)')
 % av=axis : xmn=av(1) : xmx=av(2) : ymn=av(3) : ymx=av(4) :
% axis([xmn xmx 0 ymx])
figure('Position',[700 100 550 500]) ; %Fig V_AD spectrum
subplot (2,1,1)
plot(freqV/le6,abs(FVV_AD))
title('Frequency Spectrum (A/D Voltage)')
xlabel('Frequency (MHz)')
ylabel('Frequency Spectrum')
subplot (2,1,2)
plot(freqV/le6,angle(FVV_AD))
title('Frequency Spectrum Phase (A/D Voltage)')
xlabel('Frequency (MHz)')
ylabel('Frequency Spectrum Phase')
N Save data as file that can be read into DATREDUC_HD programs (real data analysis)
savdat - V_AD*
save HDPS.txt -ascii savdat
```

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